

**A METHOD FOR GRAVITY AND MAGNETIC DATA INVERSION USING
VECTOR AND TENSOR DATA WITH SEISMIC IMAGING AND
GEOPRESSURE PREDICTION FOR OIL, GAS AND MINERAL
EXPLORATION AND PRODUCTION**

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BACKGROUND OF THE INVENTION

Field of the Invention

The present invention pertains to processing gravity and magnetic data using
vector and tensor data along with seismic data and more particularly to the inversion
of gravity and magnetic data and combining with seismic data for hydrocarbon
exploration and development, and to detect abnormally pressured subterranean
formations in general, and with specific application to areas underneath and around
anomalies such as salt, igneous or magmatic formations.

Related Prior Art

In exploration for hydrocarbons in subsurface environments containing
anomalous density variations has always presented problems for traditional seismic
imaging techniques by concealing geologic structures beneath zones of anomalous
density. Many methods for delineating the extent of the highly anomalous density
zones exist.

United States patent number 4,987,561, titled "Seismic Imaging of Steeply
Dipping Geologic Interfaces, issued to David W. Bell, provides an excellent method
for determining the side boundary of a highly anomalous density zone. This patent
locates and identifies steeply dipping subsurfaces from seismic reflection data by first
identifying select data which have characteristics indicating that seismic pulses have

been reflected from both a substantially horizontal and a steeply dipping interface. These data are analyzed and processed to locate the steeply dipping interface. The processed data are displayed to illustrate the location and dip of the interface. This patent, while helping locate the boundaries, provides nothing to identify the subsurface formations on both sides of the boundary.

There have also been methods for identifying subsurface formations beneath anomalous zones using only seismic data to create a model and processing the data to identify formations in light of the model. By further processing reflection seismic data, the original model is modified or adjusted to more closely approximate reality.

An example of further processing seismic data to improve a model is United States patent number 4,964,103, titled "Three Dimensional Before Stack Depth Migration of Two Dimensional or Three Dimensional Data," issued to James H. Johnson. This patent provides a method of creating a three-dimensional model from two dimensional seismic data. This is done by providing a method of ray tracing to move before stack trace segments to their approximate three-dimensional position. The trace segments are scaled to depth, binned, stacked and compared to the seismic model. The model can then be changed to match the depth trace segments that will be stacked better, moved closer to their correct three-dimensional position and will compare better to the model. This patent uses a rather extensive seismic process to modify a seismic model that is not accurate.

One source of geologic exploration data that has not been used extensively in the past is potential fields data, such as gravity and magnetic data, both vector and tensor data and using potential fields data in combination with seismic data to provide a more accurate depth model or to derive a velocity model.

Gravity gradiometry has been in existence for many years although the more sophisticated versions have been held as military secret until recently. The measurement of gravity has become more acceptable in the late eighteen hundreds when measuring instruments with greater sensitivity were developed. Prior to this

time, while gravity could be measured, variations in gravity caused by the effect of a large nearby object at one location, the gravity gradient, could not be reliably measured.

5 It has been known since the time of Sir Isaac Newton that bodies having mass exert a force on each other. The measurement of this force can identify large objects having a change in density even though the object is buried beneath the earth's surface or in other ways out of sight.

10 Exploration for hydrocarbons in subsurface environments containing anomalous density variations such as salt formations, shale diapirs and high pressure zones create havoc on seismic imaging techniques by concealing geologic structures beneath zones of anomalous density. By utilizing gravity, magnetic and tensor gravity field measurements along with a robust inversion process, these anomalous
15 density zones can be modeled. The spatial resolution obtained from this process is normally much lower resolution than that obtained from reflection seismic data. However, models obtained from gravity and magnetic data can provide a more accurate starting model for the seismic processing. Using the potential fields data models as a starting point for two dimensional and three dimensional seismic depth
20 imaging greatly enhances the probability of mapping these concealed geologic structures beneath the zones of anomalous density.

 Zones of anomalous density may also be associated with zones of anomalous fluid pressure. Typically, while drilling an oil or gas well, the density of the drilling
25 mud must be controlled so that its hydrostatic pressure is not less than the pore fluid pressure in any formation along the uncased borehole. Otherwise, formation fluid may flow into the wellbore, and cause a "kick." Kicks can lead to blowouts if the flow is not stopped before the formation fluid reaches the top of the well. If the fluid contains hydrocarbons, there is a serious risk of an explosion triggered by a spark. For
30 this reason, wellbores are drilled with a slight excess of the borehole fluid pressure over the formation fluid pressure.

A large excess of the borehole fluid pressure over the formation fluid pressure, on the other hand, is also undesirable. Fractures in the borehole wall may result in loss of circulation of the drilling fluid, resulting in stuck drill strings. Even if drilling can be continued, it is slowed down, resulting in greater costs. Serious formation damage may also occur.

Pressure prediction is done by estimating certain key parameters that include the overburden stress or confining stress, which is defined as the total lithostatic load on a rock volume at a given depth, and the effective stress, which is defined as the net load on the grain framework of the rock at a given depth. These two relations are then used in the Terzaghi effective stress law to estimate the fluid or pore pressure. Terzaghi's law states that:

$$P_c = P_e + P_p$$

where:

(P_c) = the confining stress

(P_e) = the stresses born by the grains, and

(P_p) = the stress born by the fluid.

Some workers treat a special case of Terzaghi's law where the confining stress is assumed to be the mean stress as opposed to the vertical confining stress. It should be acknowledged that this difference exists, but that it does not effect the embodiments of the present invention as they will pertain to estimating the total overburden load, which can then be converted to either vertical confining stress or mean stress based on the stress state assumptions that are made. The current prior art used for estimating confining stress is to use a density log from a nearby calibration well and integrate the density data to obtain the overburden load. This calibration was then applied from the mudline down to depths usually beyond the depth of sampling to predict the overburden away from the calibration well.

It has long been recognized that velocities of seismic waves through sedimentary formations are a function of "effective stress," defined as the difference

between the stress caused by the overburden and the pore fluid pressure. A number of methods have been used to measure the seismic velocities through underground formations and make an estimate of the formation fluid pressure from the measured velocities. *Plumley* (1980) and United States Patent 5,200,929 issued to *Bowers*, (the '929 patent) describe a method for estimating the pore fluid pressure at a specified location. The method also accounts for possible hysteresis effects due to unloading of the rock formation. The method utilized a pair of sonic velocity-effective stress relations. One relationship is for formations in which the current effective stress is the highest ever experienced. A second relationship is used when the effective stress has been reduced from the maximum effective stress experienced by the rock and hysteresis must be accounted for.

The '929 patent uses density data from nearby wells or from a geologically similar well to obtain the overburden stress. In most circumstances, the overburden stress may be adequately described by general compaction models in which the density increases with depth, giving rise to a corresponding relation for the relation between depth and overburden. In the absence of well control, determination of the overburden stress even within a sedimentary column is problematic. Furthermore, there are circumstances in which the model of a density that increases uniformly with depth is not valid. In such cases, the assumption of increasing density with depth is violated and a different approach to estimation of the overburden stress is needed.

There are several types of situations that may arise wherein a model of density increasing with depth and compaction is not valid. In the first case, there is a region of abnormally high density in the subsurface, usually of magmatic origin. The region could consist of an extrusive or intrusive volcanic material having relative density of 2.8 or higher. When such a formation is present within a sedimentary section where the relative density is typically between 2.4 and 2.65, the result is an increase in the overburden stress underneath the formation over what would be determined by prior art calculations. On the other hand, a region of abnormally low density may occur from salt bodies (2.10) or shale diapirs. In such a case, the overburden stress is abnormally low compared to what would be determined by prior art methods. In

either case, even if the effective stress could be determined from seismic velocity measurements, a formation fluid pressure determination based on a prior art density model would be invalid.

5 In prior art, it is common to extrapolate away from a control well to derive an initial pressure model. When abnormally pressured sediments are present having higher porosity and lower density than sediments in the control well, the model of increasing density with depth is violated and the confining pressure is overestimated. There is a need for a method to image subterranean formations which are responsive
10 to potential fields and non-potential fields data. The present invention combines these data types to extract more useful information than either data type has provided before.

 There is a need for a method for accurate determination of fluid pressures in
15 the subsurface that (1) does not require the availability of density logs and (2) can more accurately determine the density of the subsurface in 2D or 3D away from and deeper than the limits of density from well control. Such a method should preferably be able to obtain fluid pressure even in the presence of anomalous formations that
20 have densities significantly different from those expected in normal sedimentary columns or that predicted by density values in single or multiple wells. The present invention satisfies this need.

SUMMARY OF THE INVENTION

25 The present invention incorporates a robust inversion process for determining parameters and geologic structure representing subterranean formations including determining subsurface formation fluid pressures using seismic data in combination with vector and tensor potential fields data, both gravity and magnetics. One or more components of potential fields vector and tensor data are measured at a plurality of
30 locations over a region including the anomalous formation. The potential fields may be either gravity fields or magnetic fields, vector and/or tensor. A geophysical model of the region including the anomalous formation is determined using gravity,

magnetics, seismic or a combination of these. A value of the one or more components of the potential fields vector and tensor data at the plurality of locations is estimated for the model. A difference between the estimated values and the measured values at the plurality of locations is determined. The model of the region is updated based on the difference. The estimate of the value of the one or more components, the determination of the difference and the updating of the model is repeated until the difference reaches a minimum value. The updated model is used to determine the parameter of interest. Abnormal densities in the subterranean formations are commonly associated with a salt body, a shale diapir, and extrusive or intrusive igneous bodies. In one embodiment the parameter of interest can be combined with seismic data representing the same parameter for depth imaging to provide a geologic depth model and to derive a velocity model. In another embodiment, seismic data can be introduced into the inversion process to further refine the lower boundary parameter predictions. The process of inversion followed by seismic imaging followed by another inversion and seismic imaging step is repeated until the results of the gravity magnetics inversion and the seismic imaging processes converge to a single answer. The seismically determined velocities give an estimate of the effective stress while the inverted density model gives the overburden stress. The difference between the overburden and the effective stress is the fluid pressure. In an alternate embodiment of the invention, the method is used to obtain density models and subsurface imaging of anomalous zones such as salt bodies, shale diapirs, and extrusive or intrusive igneous bodies, where seismic data alone is unable to obtain accurate velocity estimates or do accurate imaging due to ray path distortions. The geometries and densities of these anomalous bodies are then used to generate improved overburden estimates compared to the prior art where only nearby well densities were used to constrain the overburden. For example, in the case of salt formations in the Gulf of Mexico, a top of a salt map derived from seismic imaging along with a density model and bathymetry, are utilized to produce a base of salt model from the inversion process. This may be used as input to the seismic data to obtain velocity (and effective stress) information underneath the anomalous zone.

BRIEF DESCRIPTION OF THE DRAWINGS

Figure 1 is a seismic section of an area having anomalous density zones such as a salt domes.

Figure 2 is a flow chart of a method for modeling geological structures beneath anomalous density zones.

Figure 3 is a graphical representation of the overall model integration illustrating a chosen window and observation points.

Figure 4 is a flow chart of an embodiment of the invention for combining seismic data and potential fields data for modeling geological structures beneath anomalous density zones.

Figure 5 is a flow chart of an alternate embodiment of the invention for combining seismic data and potential fields data for modeling geological structures beneath anomalous density zones.

Figure 6 is a flow chart of an embodiment of the invention for combining seismic data and potential fields data.

Figure 7 is a flow chart of an embodiment of the invention for determining fluid pressure in a region of interest.

Figure 8 is a flow chart of an embodiment of the invention for determining fluid pressure below a subterranean formation of interest, like an body with anomalous density or velocity.

DESCRIPTION OF THE PREFERRED EMBODIMENT

The present invention utilizes a very robust formulation for calculating gravity, magnetic and tensor fields due to a parameterized model such as salt formations embedded in a known or assumed distribution of sediments. The embedded model is composed of an upper boundary, usually mapped with seismic methods, and a parameterized lower boundary to be determined by an inversion process. The parameterized lower boundary first uses gravity and magnetic data to predict parameters. Then, seismic data can be combined to provide a depth image using the predicted parameters as the driver. Further, a velocity model can be derived using the predicted parameters. In the alternative, the seismic data may be used as an

additional constraint in running the inversion process again. This process of inversion followed by seismic imaging followed by another inversion and seismic imaging step may be repeated until the results of the gravity magnetics inversion and the seismic imaging processes converge to a single answer or a point of diminishing returns is reached. Otherwise, if the process results begin to diverge indicating that there is not a unique solution, the process is discontinued.

Co-pending United States Patent Application No. 09/285,570, No. 09/399,218 and No. 09/405,850 having the same assignee and the contents of which are fully incorporated here by reference, discloses a method and apparatus in which a gravity and magnetics inversion technique developed for use with gravity, Full Tensor Gradiometry (FTG) gravity and magnetics can be used as a driver for building earth models for seismic data processing. Some of the disclosure of the '570, '218 and '850 applications are included here for convenience.

This formulation of the present invention makes it possible to build an inversion process to predict the lower boundary parameters so as to minimize the difference between any or all of the model fields mentioned above and their measured counterparts. Since this inversion process is so robust and applicable to so many varied field measurements, it is proving to be useful for exploration at both regional and prospect scales.

The inversion process of the present invention demonstrates its strength in several areas. In the area of background sediment properties, the density and susceptibility can have any horizontal variability including discontinuities. The depth variation of these properties is assumed to be a polynomial up to order six for density and order five for susceptibility. Thus, for practical purposes, there are no apparent restrictions on the variability of density and susceptibility especially considering the inherent resolution of gravity and magnetic analyses.

For three dimensional inversion, the forward model fields and associated sensitivity matrix components, (partial derivatives of the model fields with respect to

the parameters representing the lower boundary), used in the inversion process can be calculated in a two dimensional integration routine simultaneously. This fact makes the three dimensional inversion tractable.

5 For two dimensional inversion, the problem can be contracted to a one dimensional integration routine allowing inversion steps to be done extremely rapidly. This inversion is used to model single profiles of field data. Two point five and two point seven five dimensional inversions are also applied to single profiles of data. Rather than assuming the model to be infinitely extended on both sides of the profile,
10 the two point five model has finite but equal extensions on both sides of the profile, whereas the two point seven five dimensional model has unequal extensions. Both types of inversions can be processed very rapidly by utilizing the three dimensional framework. Furthermore, this allows off profile variations of the model to be entertained by either predicting them in the inversion process or by setting them a
15 priori based on seismic and/or other available information.

 Computations based on parallel computing techniques were investigated only for the three dimensional case since the two dimensional, two point five dimensional and two point seven five dimensional inversions are already fast. It turns out that the
20 way the inversion process is setup, it is ideal for using multiple processors. Thus, the elapsed time previously required for large three dimensional inversion processes can be greatly reduced. This is especially important for regional studies where large data sets are required.

25 For data preparation, the forward modeling portion of this inversion software is also used to correct the gravity, magnetic and tensor data for complex bathymetric effects. Bouguer corrections are made assuming a depth dependant density as discussed in background sediment properties in order to obtain better input gravity and tensor data for the inversion process. This represents a substantial improvement
30 over the standard use of a constant Bouguer density.

 Those versed in the art would recognize that numerous corrections are applied

to magnetic data measurements to get a better representation of the magnetic field. These include a diurnal correction to correct for magnetic field variations during the day, an International Geomagnetic Reference Field (IGRF) correction, and a leveling correction to resolve misties between data acquired at different times. The present
5 method works equally well whether or not a reduction to pole correction is made: such a correction corrects for the effect of an anomalous body depending upon its position with respect to the magnetic poles of the earth.

Some of the major problems confronting the application of any modeling
10 technique applied to potential field data is the removal of the regional field and, thus, the isolation of the field believed to be associated with the scale of the model being examined. By properly filtering the data between successive iterations in the inversion process, predicted regional fields can be obtained for the gravity and magnetic data sets simultaneously, thus allowing convergence to a common model
15 structure that explains both the band-limited gravity and magnetic fields associated with the anomalous body. The resulting regional fields then can be modeled to predict deep seated structures beneath the area of immediate interest.

Part of the inversion process that dramatically improves the convergence and
20 efficiency of the algorithm is a predictive filtering procedure that reconstructs the regional field from the inversion itself. At each inversion step, the inversion estimates the anomalous body model that is required to fit the data and compares this model response to the observed field. The difference between the model and the observed field is treated as a "residual" or "error", the long wavelength component of
25 this error field is calculated and attributed to the regional field that must be accounted for in the regional model. This long wavelength residual is used to reconstruct the regional model and this reconstructed regional model is compared to the long-wavelength regional component that is removed early in the preprocessing of the potential fields data to make sure that the signal used in the inversion was properly
30 separated between signal related to the anomalous bodies and that related to the regional field.

The present invention also includes a step for processing the tensor data to make sure that the data are consistent in the model that they will invert to. Effectively, this is a process where a flat model is used and densities are imbedded in the model to properly determine the long-wavelength filter that must be applied to the data so that the Laplace Equation is not violated when the inversion is run. This contrasts with prior art methods that use a simple band-pass filter to remove the long wavelengths and derive a residual field. If that is done blindly in the same way for each tensor component, the answer will be wrong because the different components of the tensor data will be inconsistent with each other and not satisfy the Laplace Equation. The new method determines the proper filter for each tensor component and then filters that component so that the earth model used to filter the 5 independent tensors is internally consistent. When this is done properly, it assures that the tensor residuals are correctly treated so that they can converge to a single earth model in the inversion process. This approach is also used to remove the high-frequency white noise as well, and is used to make the entire frequency band in the residual field consistent.

All tests of this invention have utilized base functions equivalent to those used in half cosine transforms for parameterizing the lower boundary in the inversion code. However, it should be emphasized that essentially any orthogonal set of functions can be substituted with minimal effort. For example, it may be found that a power series or Legendre polynomials may provide better convergence in the inverse process.

Other tests of orthogonal basis functions have utilized the Daubechies wavelet set DAUB4 for parameterizing the lower boundary of the subterranean formation of interest. A sliding boxcar function with variable width has also been used.

An important aspect of this invention is that the observation positions can be distributed arbitrarily, thus removing the need to have the data in a gridded form on the same datum. This is especially important when simultaneously inverting data sets from various contractors. Also, individual field observations can be weighted in the inversion process according to their uncertainty.

Figure 1 is a seismic section illustrating an area of interest having highly anomalous density zones such as a salt domes. A rounded interface can be seen as masking the formations below. For this data set, the lower boundary can not be determined by normal seismic data processing methods.

Referring now to Figure 2, a flow chart illustrates a method for providing a model upon which derivation of subsurface formations can be based. At block 12 reflection seismic data is received. In general, reflection seismic data is more reliable than other forms of geologic exploration data in most situations because of the extensive work and research that has been devoted to its use and application.

At block 14, the reflection seismic data is used to derive the top portion of a geologic model. As stated previously, reflection seismic data is very reliable, at least in this situation, for determining a model containing the top of an anomalous density zones. Geologic boundaries beneath the top of the anomalous are not as easily modeled. While reflection seismic data is generally more reliable than other forms of geological surveying, anomalous density zones, such as a salt dome, block or highly distort reflection information below the zone. In this type of area reflection seismic surveying becomes unreliable, as shown in this example. In some cases, the reflection seismic data becomes so unreliable that no information at all below the salt dome can be obtained from reflection seismic exploration.

At block 16, data pertaining to the determination of the lower boundary is received. This data may take the form any potential fields data, both vector and tensor. In the formulation used, the type of data is of no concern since any combination of the above mentioned data can be processed simultaneously. Although these types of data are generally provide less resolution than reflection seismic data, in this case, of an anomalous density zone, potential field data provide the most reliable starting point.

The data received are used to formulate the limits of the lower boundary for

the geologic model block 18. The actual derivation of the lower boundary is done by predicting parameters representing the lower boundary through an inversion process.

5 Although various inversion techniques can be utilized to determine the parameters (coefficients) representing the lower boundary, the particular one tested in the present invention involves the successive inversion of a single coefficient at a time until all coefficients are determined. The total number of coefficients is set a priori at block 18 based upon the minimum wavelength (maximum frequency) desired
10 in the lower boundary. Typical lower boundaries will contain as many as nine hundred coefficients for three-dimensional models, thirty in each horizontal direction. For example, if x_1 and x_2 are the spatial limits of integration in the x direction and y_1 and y_2 are the spatial limits of integration in the y direction, and half cosine series are used, the number of terms required in the x and y directions respectively for a
15 minimum wavelength of $\lambda_{\min}$ are:

$$n_x = \frac{2(x_2 - x_1)}{\lambda_{\min}} + 1 \quad (1)$$

and

$$n_y = \frac{2(y_2 - y_1)}{\lambda_{\min}} + 1 \quad (2)$$

20

Thus the total number of coefficients representing the lower boundary is n_x times n_y .

25

At block 20, the first coefficient representing a uniform lower boundary (longest wavelength component) is predicted. This coefficient is based on the received data and represents the best fit possible with limited information.

At block 22 another coefficient is added through the inversion process. At

block 24 all coefficients added thus far are readjusted through single parameter inversion in the order in which they were added to the lower boundary (from the longest to the shortest wavelength coefficients). This process continues until all coefficients (n_x times n_y) have been predicted. At decision block 26 a determination is made as to whether all coefficients have been predicted. If they have not, the program returns to block 22 where another coefficient is added.

If all coefficients have been predicted, the program proceeds to block 28 where the lower boundary is displayed. This display may take any form currently in use in the art, such as a monitor display, a hard copy printout or be kept electronically on tape or disc.

The numerical integrations necessary for each step of the overall inversion process are accomplished using a two dimensional Gaussian quadrature for the two horizontal variables while the vertical integration is usually done analytically. Any or all of the components of the potential fields fields vectors and tensors, along with their respective partial derivatives (with respect to each of the coefficients associated with the lower boundary) are integrated simultaneously for each observation, thus saving substantial computer time. Furthermore, between each inversion for estimating a given coefficient an updated integration mask is produced to restrict the integration to the anomalous density region of the model. Another mask (not shown) is utilized for each observation point to limit the horizontal extent of the integration in order to further conserve computer time. This is especially important since as many as one hundred thousand numerical integrations per observation point per component are performed, each using about one hundred thousand Gaussian nodes. Thus, for typical exploration applications, billions of integrations are necessary.

For Gaussian integration the integral is broken up into k intervals and the two point Gaussian quadrature is applied to each interval. For example, the j th interval is:

$$\int_{a_j}^{b_j} f(x) d(x) = \frac{(b_k - a_k)}{2} \sum_{i=1}^2 w_i f(x_i) \quad (3)$$

where $w_i = 1.0$, and

$$x_i = \frac{(b_k - a_k)}{2} x_i' + \frac{(b_k + a_k)}{2} \quad (4)$$

5

with x_i' being simply:

$$x_1' = -x_2' = -\frac{1}{\sqrt{3}}$$

Thus, the total integral is

$$10 \quad I = \sum_{k=1}^K \int_{a_k}^{b_k} f(x) d(x) \quad (5)$$

This is easily extended to two dimensions as follows:

$$I = \sum_{k=1}^K \sum_{l=1}^L \int_{a_k}^{b_k} \int_{a_l}^{b_l} f(x, y) dx dy \quad (6)$$

where

$$\int_{a_k}^{b_k} \int_{a_l}^{b_l} f(x, y) dx dy = \frac{(b_k - a_k)(b_l - a_l)}{4} \sum_{i=1}^2 \sum_{j=1}^2 w_i w_j f(x_i, y_j) \quad (7)$$

15

with $w_i = w_j = 1.0$, and, as before,

$$x_i = \frac{(b_k - a_k)}{2} x_i' + \frac{(b_k + a_k)}{2}$$

and

$$y_j = \frac{(b_l - a_l)}{2} y'_j + \frac{(b_l + a_l)}{2}$$

where $x_1 = y'_j$, and $x_2 = -x_1 = 1/\sqrt{3}$

Thus, the entire integration process is controlled by determining the number of intervals K and L that are used to represent the overall integration limits of x and y and, therefore the values for the a_k , b_k , a_l and b_l .

Referring now to Figure 3, the overall model integration is illustrated. The overall integration is $x_1 \rightarrow x_2$ and $y_1 \rightarrow y_2$. As illustrated, each observation point A can have a chosen window of integration bcde that is equal to or smaller than the model integration window.

The model window of integration is broken up into K times L, a two by two Gaussian quadrature. The dimensions are given by $(x_2 - x_1)/K$ units by $(y_2 - y_1)/L$ units. Thus, the interval for the Gaussian points x_i and y_i will be approximately one half of these respectively.

All information about the distribution of the Gaussian points is calculated prior to the actual calculation along with which Gaussian points have to be utilized for model integration at each observation point. This helps make the problem of doing inversion in the spatial domain tractable.

For a given distribution of Gaussian intervals the variable boxcar function can straddle any number of these intervals in the x and y directions. Widths of one interval in each direction yielding four Gaussian nodes in each window or cell work well. Assume the base or lower boundary is flat and parameterized at a depth determined by the inversion process. For a region covered by 500 by 500 Gaussian intervals one would have 250,000 parameters to solve for, given a window size would be one by one intervals. For the case of a DAUB4 wavelet function the minimum window size would be two by two intervals with a 50% overlap of windows, thus

producing approximately the same number of unknown parameters which, in this case, are the coefficients of the 2-D wavelets. The vertical integration is accomplished by either solving for an analytical expression to take into account the variation of sediment properties with depth or by numerically integrating an analytical or digital expression for these properties. The digital expression would be in the form of a density and susceptibility cube.

There are a number of techniques to solve problems with numbers in the tens of thousands. A simple method that gives very good results is to invert on one parameter at a time chosen randomly. This removes large memory and cpu requirements. A psuedo-annealing process is applied by only allowing a small change in each parameter to take place during each iteration. After all parameters have been processed, a low-pass filter is applied to the surface. The iteration process is continued until an acceptable model is obtained. The randomization process between each iteration is accomplished via a random number generator. Typical inversion times are reduced with this invention from days and hours down to a matter of minutes for typical study areas.

Referring now to **Figure 4**, a flow chart illustrating a method for combining seismic and potential fields data to provide a model upon which derivation of subsurface formations can be based. This method uses the method of **Figure 2** with the addition of combining seismic data once the lower boundary has been predicted by the potential fields inversion. The method of **Figure 2** will be briefly repeated to illustrate how the combination with seismic data is accomplished. At block 12 reflection seismic data is received to begin the modeling procedure.

At block 14, the reflection seismic data is used to derive the top portion of a geologic model. As stated previously, reflection seismic data is reliable for determining the top of highly anomalous density zones. While the top portion of the model can be accurately derived using seismic data, deeper geologic features are harder to model because highly anomalous density zones block or highly distort reflection information. At block 16, data pertaining to the determination of a lower

boundary is received. This data may be any potential fields data, both vector and tensor.

5 The received data are used to formulate the limits of a lower boundary for the geologic model for the area of interest at block 18. The lower boundary is predicted through an inversion process, as described above.

10 At block 20, the first coefficient representing a uniform lower boundary (longest wavelength component) is predicted. This coefficient is based on the received data and represents the best possible fit with limited information.

15 At block 22 another coefficient is added through the inversion process. At block 24 all coefficients added thus far are readjusted through single parameter inversion in the order in which they were added to the lower boundary (from the longest to the shortest wavelength coefficients). This process continues until all coefficients (n_x times n_y) have been predicted. At decision block 26 a determination is made as to whether all coefficients have been predicted. If they have not, the program returns to block 22 where another coefficient is added.

20 If all coefficients have been predicted, the program proceeds to block 30 where the predicted lower boundary is combined with seismic data representing the area of the lower boundary. The result of the inversion process produces an earth model that contains the geometric description of three dimensional and two dimensional lithologic bodies with anomalous density and velocity. These geometries and the assigned velocities and densities can be used as an input to pre- and post-stacking processing steps that require a geometrically correct velocity model. At this time, the predicted parameters for the lower boundary can be used as a driver for depth imaging.

30 The output at this point is a model in which the lower boundaries of the anomalous zone and its density have been determined. Knowing the density of the anomalous zone and known relationships between the density of different types of

rock types and the velocity of elastic waves in such rocks, an updated velocity model may be obtained. This is done at block 32. The model may then be used as input to seismic processing methods, for example, velocity analysis, Kirchhoff migration, Dip Moveout (DMO), finite difference migration, F-X migration, etc., to improve velocity estimates as well as depth and time images of the subsurface.

Once new models have been formulated, the program proceeds to block 34 where the newly derived model using the gravity/magnetic data is displayed. This display may take any form currently in use in the art, such as a monitor display, a hard copy printout or be kept electronically on tape or disc or other suitable storage medium.

Referring now to Figure 5, a flow chart illustrates a second method for combining seismic and potential fields data to provide a model upon which derivation of subsurface formations. This method uses the method of Figure 2 and a portion of the method of Figure 4 with the addition of combining seismic data once the lower boundary has been predicted. The basic method of Figure 2 will be repeated briefly again to illustrate how the combination of the inversion process with seismic data is accomplished.

At block 14, the reflection seismic data received at block 12, is used to derive the top portion of a geologic model. At block 16, data pertaining to the determination of the lower boundary are received. These data may take the form of any potential fields data, both vector and tensor. Next, at block 18, the data received at block 16 are used to formulate the limits of a lower boundary for the geologic model for the area of interest as previously described.

At block 20, the first coefficient representing a uniform lower boundary (longest wavelength component) is predicted. This coefficient is based on the received data and represents the best possible fit possible with limited information.

At block 22 another coefficient is added through the inversion process. At block 24

all coefficients added thus far are readjusted through single parameter inversion in the order in which they were added to the lower boundary (from the longest to the shortest wavelength coefficients). This process continues until all coefficients (n_x times n_y) have been predicted. At decision 26 a determination is made as to whether
5 all coefficients have been predicted. If they have not, the program returns to 22 where another coefficient is added.

If all coefficients have been predicted, the program proceeds to block 34 where The Gravity Magnetic Inversion ("GMI") final model is compared with the
10 evolving seismic interpretation. The GMI model provides as an additional constraint to refine the velocity model used for imaging the seismic data. Combining the gravity magnetic inversion result with the seismic data represents the beginning of a sub process that uses the inversion results as a starting earth model to derive an improved seismic image beneath the density anomaly .

15 At block 36, the seismic velocity model is updated. The model may be obtained as described above with reference to Figure 4. In this step, the result of the inversion is used to drive the seismic imaging process. At block 38, depth imaging is performed using the updated seismic velocity model to better define the base of the
20 anomalous body and underlying structure. However, portions of the subsurface may still be poorly imaged by the seismic data, partly due to errors that still remain in the evolving velocity model.

At block 40, the seismic reflection data from the base of the anomalous body
25 is interpreted and mapped to produce an updated model for further analysis. GMI can be performed again with the new model as a constraint to solve for the remaining portions of the anomalous body that were not imaged in step 38 using the seismic data.

30 At block 42, the base as interpreted from the seismic reflection data is compared to the base predicted by the gravity magnetic data inversion process. A determination is made in block 44 as to whether the seismic model and the gravity

magnetic model agree. If they do not agree, the process proceeds to block 46 where the GMI model is updated with the new seismic constraints in regions where the base of the anomalous body is well imaged. The process returns to block 20 to perform the inversion process again with the new constraints. This process of inversion followed by seismic imaging followed by another inversion and seismic imaging step is repeated until the results of the gravity-magnetics inversion and the seismic imaging processes converge to a single answer.

If the seismic model and the gravity magnetic model do not converge or begin to diverge, there is not a single solution consistent with all the input data. At this time the process may be terminated since the process is not having desired results. This may be due to either poor quality seismic data or some other problem with the received data. If the seismic model and the gravity magnetic model do agree, the process proceeds to block 48 where the process is ended and the model may be displayed.

Turning now to Figure 6, the main steps of a method for combined inversion of potential fields data and seismic data are shown. The region of earth being studied is not limited to areas of anomalous density.

Seismic data in block 101 are used for deriving an initial geophysical model in block 105. This is done by forming a seismic depth image of the subsurface structure and using subsurface velocities and/or well logs for an initial estimate of the densities. Based upon the geophysical model, a prediction is made of the gravity/magnetic data in block 109. Separately, the gravity/magnetic data, block 103, are preprocessed as described above. A comparison is made between the predicted values of the gravity/magnetic data and the actual values and this difference is compared to a set threshold in block 111. If the difference is small, block 113, then the density model of the subsurface is suitable for additional interpretation of the seismic data. If the difference is large, then an inversion of the gravity/magnetic data is performed in block 115 to give an updated geophysical model, block 115, and processing goes back to block 109.

A number of embodiments of the present invention have been described. In one embodiment, the predicted parameters are combined with seismic data to obtain a depth image and a velocity model for delineating formations of interest. In a second embodiment, imaging of the seismic data is performed using a lower boundary
5 determined from the initial inversion. This seismic result is mapped to determine the position of the base of the anomalous body and is compared to the model parameters to obtain a difference between the two. The parameters are adjusted to provide a best fit. A new model is formed based on the new predicted parameters, and the GMI and seismic imaging are iterated until the solution converges.

10

Referring to Figure 7, the main steps involved in the present method of determination of subterranean fluid pressure are shown. The method uses two main types of data. The first type of data comes from a seismic survey, block 801, acquired over the area of interest. This may be in a land or marine environment and,
15 using methods known in the art, the seismic data are processed to give an initial model of seismic velocities for the subsurface, block 805. The second type of data is acquired from a potential fields data survey, block 803. This type of data that has not been used extensively in the past for subsurface fluid pressure prediction. It includes both vector and tensor components of gravity and magnetic data. Optionally, density
20 information, such as well logs, block 802, may also be used. The use of density logs is discussed below.

As discussed below, the potential fields data are used in determining the fluid pressure in subsurface formations. The spatial resolution obtained from this process
25 is normally much lower than that obtained from reflection seismic data. However, models obtained from gravity and magnetic data can provide a more accurate determination of subsurface overburden loads.

The initially derived seismic velocity model is used to obtain an initial
30 estimate of subsurface structure. Additionally, it may be used to obtain the density distribution in the subsurface using known methods, block 807. For example, Gardner (1974) has derived an empirical relation between the density of commonly

observed subsurface sedimentary rock types and the velocity of propagation of seismic waves through the rocks. Alternatively, the initial values of density may be obtained using supplemental information such as density logs, block 802, from nearby wells. Density logs may be used directly as input to the density model or used with velocity data to fit a locally-calibrated Gardner relationship for a specific area. The use of the well control in conjunction with a seismic structure map makes it possible to extrapolate densities from the wells to the area of interest.

In the present invention, the method of Figure 2 is used with the initial density model, block 807, and certain constraints on the allowable densities in the inversion process to obtain a density model for the subsurface in 809. The constraints in the present invention limit the allowable values in the inversion process to a range of values around the initial density model 807.

The result of the inversion comprises a model of the density of the subsurface of the earth. This density model is then integrated with respect to depth using known methods to obtain values for the overburden stresses in the subsurface 815.

Using the velocities derived at 805, the effective stresses in the subterranean formations are determined 813. One method for relating the interval velocity V to the effective stress is a relationship of the form

$$V = C + A\sigma^B \quad (8)$$

where V is the interval velocity, and A , B and C are determined empirically from observations. Typically, the value of C is approximately 5000 ft/s.

Other relations between the velocity and the effective stress could also be used. For example, *Gassmann* (1951) showed that for a packing of elastic spheres, the bulk modulus of the packing β is proportional to the two-thirds power of the effective stress.

$$\beta \propto (P_e)^{2/3} \quad (9)$$

The compressional velocity V_p is related to the bulk modulus by the relation

$$V_p = \left(\frac{\beta}{\rho} \right)^{1/2} \quad (10)$$

5 Where ρ is the density. Empirically, the value of the exponent B in equation (8) is usually found to be close to 1/3, which is consistent with the value predicted by *Gassman's* model calculations in equations (9) and (10).

10 While a packing of elastic spheres is not a good representation of sedimentary rocks, the power law is nevertheless generally accepted to be a good empirical relation between effective stress and the compressional wave (P- wave) velocity of a rock. For example, *Hamilton* (1976), shows empirical data of compressional and shear velocities of water saturated sands as a function of effective stress. The data are consistent with a power law relation between velocity and effective stress.

15 Returning to Figure 7, the difference between the overburden stress 815 and the effective stress 813 is determined 817 to give an estimate of the fluid pressure in the subsurface 819. This estimated fluid pressure may be used to guide the drilling process by, e.g., selecting a suitable mud weight in the borehole to avoid the risk of a kick or a blowout. Under normal conditions, the mud weight is chosen so that the pressure exerted by the column of mud in the borehole is slightly in excess of the fluid pressure in the formation but less than the pressure that could cause formation damage by forcing drilling mud into the formation through fracture failure.

20 Accordingly, if the determined formation fluid pressure at any projected depth during the drilling of the borehole is abnormally low, the mud weight is reduced to avoid formation damage. Conversely, if the determined formation fluid pressure is abnormally high, the mud weight used in drilling is increased to avoid the danger of a kick.

30

In drilling operations, the mud is circulated down the drillstring to the drillbit and returns up to the surface through the annulus between the drillstring and the borehole. Those versed in the art would recognize that even if the mud weight is selected so as to not cause formation damage under static conditions, this may not be sufficient to maintain borehole integrity under dynamic conditions. During drilling, the mud pressure at the bottom of the borehole has to be sufficient to enable the mud returning from the bottom of the borehole to overcome frictional losses in the borehole, so that the bottom hole mud pressure will exceed the hydrostatic pressure of the formation. This may be sufficient to fracture the formation at the bottom hole. Accordingly, it is necessary to monitor a number of different parameters, such as flow rate of the mud, in addition to the mud weight, to maintain the integrity of the borehole. The flow rate of the mud in turn limits the weight on bit, the rate of penetration and the torque on the bit. These parameters are controlled based upon knowledge of the formation fluid pressure obtained in the present invention.

Figure 8 discloses an alternative embodiment of the invention wherein the subsurface includes an anomalous region in which the seismic velocity and/or density is significantly different from that of the neighboring regions. An example of such an anomalous region is a salt body. As would be known to those versed in the art, a salt body has a significantly different seismic velocity than other sedimentary formations which surround the salt, making it difficult to obtain seismic images or seismic velocities below the salt body. Starting with the seismic data, block 901, an initial determination of seismic velocities to the top of the anomalous zone is made in block 905. This, as discussed with reference to Figure 7 above, is used to derive an initial geophysical model to the top of the anomalous zone, block 907. The geophysical model includes density information that is derived either from seismic velocities or from well logs, block 902. The initial model also includes an initial estimate for the density of the anomalous zone. This is generally straightforward as the type and density of the rock in the anomalous zone would be known from geological considerations. For example, salt has a density of 2.10 g/cc and a seismic velocity of 14200 ft/s.

Using the method described above with reference to Figure 2, the potential fields data, block 903, are inverted in block 909. The difference from this step and the inversion step, block 809, of Figure 7 is that here, the inversion is carried out to define the base of the anomalous zone. This inverted model also constrains a velocity model for the anomalous zone: as noted above, the seismic velocities for the common types of anomalies are known. More importantly, the inversion gives an estimate of the lower boundary of the anomalous zone that can be included in an improved velocity model of the entire anomalous zone, block 913. It is then possible to use the inverted model in an improved processing of the seismic data to obtain better estimate of seismic velocities below the anomalous zone. The density model, block 911, is integrated vertically to give an overburden stress, block 912. That overburden can be combined with the seismic velocities, block 915, to determine formation fluid pressures using the method described above with reference to Figure 7.

Where the anomalous region is a salt body, it is commonly a result of gravity-driven diapiric flow of the salt into higher density sediments. Those versed in the art would recognize, since salt is lighter than the surrounding sedimentary formations, that there would be an unloading of the overburden stress and hysteresis effects must be accounted for.

When a formation is buried and subjected to increasing depths of burial and stress, the velocity increases as expected by a model such as equation (8) or (9). When the overburden stress is reduced, either by uplift or by intrusion of salt that has a lower density than the surrounding sediments, the velocity only partially decreases, so that the velocity is higher than that given for a normally-compacted rock at the same effective stress. This hysteresis effect has been described above.

Where the anomalous body is a volcanic intrusive or extrusive body that has higher density than the surrounding sedimentary formations, the overburden stress will be higher than would be expected in a comparable depth of sedimentary rocks. The present invention is able to account for the effects of zones of anomalous density

by determining the actual density, whereas prior art methods assume that density increases uniformly with depth or varies with depth based on limited well information.

5

While there has been illustrated and described particular embodiments of the present invention, it will be appreciated that numerous changes and modifications will occur to those skilled in the art, and it is intended in the appended claims to cover all those changes and modifications which fall within the true spirit and scope of the present invention.

10

**CLAIMS**

What is claimed is:

- 1 1. A method for determining a parameter of interest of a region of interest of the
2 earth, the method comprising:
 - 3 (a) measuring at least one component of potential fields data at a plurality
4 of locations over a region of interest including a subterranean
5 formation of interest, said potential fields data selected from magnetic
6 data and gravity data;
 - 7 (b) determining an initial geophysical model of the region including the
8 subterranean formation of interest;
 - 9 (c) for said model, estimating a value of said at least one component of
10 geophysical tensor data at said plurality of locations;
 - 11 (d) determining a difference between said estimated value and said
12 measured value of said measurements at said plurality of locations;
 - 13 (e) updating the geophysical model of the region based on said difference;
 - 14 (f) iteratively repeating steps c - e until said difference is less than a
15 predetermined value; and
 - 16 (g) using said updated model to determine the parameter of interest.
- 1 2. The method of claim 1 wherein determining the initial geophysical model
2 further comprises acquiring and processing seismic data over the region of
3 interest and using the seismic data to derive the geophysical model therefrom.
- 1 3. The method of claim 2 wherein processing the seismic data further comprises:
 - 2 (i) determining seismic velocities in the region from the acquired seismic
3 data; and
 - 4 (ii) using an empirical relation between seismic velocities and densities in
5 determining a geophysical model of density.
- 1 4. The method of claim 1 wherein the region of interest includes an anomalous



- 2 subterranean formation and deriving the initial geophysical model includes an
3 upper boundary of the anomalous subterranean formation.
- 1 5. The method of claim 2 further comprising using the determined parameter of
2 interest for processing the seismic data over the region of interest to obtain an
3 image of said region of interest.
- 1 6. The method of claim 2 further comprising using the determined parameter of
2 interest for processing of the seismic data giving updated seismic data.
- 1 7. The method of claim 1 further comprising using the determined parameter of
2 interest for guiding a drilling process used for drilling a borehole in the region
3 of interest.
- 1 8. The method of claim 1 wherein the subterranean formation of interest is one
2 of the group consisting of (i) a salt body, (ii) a shale diapir, (iii) a volcanic
3 flow, (iv) an intrusive igneous body, and, (v) an extrusive igneous body.
- 1 9. The method of claim 1 wherein the at least one component comprises at least
2 two components of potential fields data, and the method further comprises
3 filtering the at least two components to give filtered data components that are
4 consistent with Laplace's equation.
- 1 10. The method of claim 1 wherein the potential fields data is at least one of (i)
2 vector gravity data, (ii) vector magnetic data, (iii) tensor gravity data, and (iv)
3 tensor magnetic data.
- 1 11. The method of claim 1 wherein the parameter of interest is selected from (i) a
2 lower boundary of a subterranean formation, (ii) a thickness of a subterranean
3 formation, (iii) a density of the subterranean formation, (iv) a magnetic
4 susceptibility of the subterranean formation, (v) a volume of the subterranean
5 formation, (vi) overburden stress in the region of interest, (vii) effective stress



6 in the region of interest, (viii) formation fluid pressure in the region of interest.
7 (ix) overburden stress below a subterranean formation of interest, (x) effective
8 stress below a subterranean formation of interest, and (xi) formation fluid
1 pressure below a subterranean formation of interest.

1 12. The method of claim 1 wherein the at least one component of potential fields
2 data is a gravity component, the method further comprising applying to the at
3 least one component of the potential fields data for at least one of (i) a latitude
4 correction, (ii) a free air correction, (iii) a fixed density Bouguer correction,
5 (iv) a variable density Bouguer correction, (v) Eotvos correction, and (vi)
6 datum correction.

1 13. The method of claim 1 wherein the at least one component of potential fields
2 data is a magnetic component, the method further comprising applying to the
3 at least one component of the potential fields data for at least one of (i) diurnal
4 correction, (ii) IGRF correction, (iii) leveling correction, (iv) bathymetric
5 correction, (v) fixed magnetic susceptibility correction, and (vi) variable
6 magnetic susceptibility correction.

1 14. The method of claim 1 wherein the model is selected from (i) a 2D model, (ii)
2 a 2.5D model, (iii) a 2.75D model, and (iv) a 3-D model.

1 15. The method of claim 1 further comprising incorporating in the model one of
2 (i) land topography, and (ii) marine sea surface and water bottom bathymetry.

1 16. The method of claim 1 wherein the determined geophysical model includes a
2 density for a portion of the region outside the subterranean formation
3 expressed as a polynomial function of depth and a laterally varying density.

1 17. The method of claim 26 wherein the density is based upon at least one of (i)
2 well log information, (ii) seismic velocity information, (iii) seismic
3 tomography, (iv) prestack seismic inversion of seismic data, (v) post-stack



4 seismic inversion of seismic data, and (vi) regional compaction curves.

1 18. The method of claim 1 wherein density of the subterranean formation in the
2 determined geophysical model is at least one of (i) a fixed density, (ii) a
3 laterally varying density, and (iii) a vertically varying density.

1 19. The method of claim 1 wherein the determined geophysical model includes a
2 magnetic susceptibility for a portion of the region outside the subterranean
3 formation of interest expressed as a polynomial function of depth and a
4 laterally varying susceptibility.

1 20. The method of claim 1 wherein the determined geophysical model includes a
2 magnetic susceptibility for the subterranean formation of interest selected that
3 is at least one of (i) a fixed susceptibility, (ii) a laterally varying susceptibility,
4 and (iii) a vertically varying susceptibility.

1 21. The method of claim 1 wherein the determined geophysical model includes a
2 base of the subterranean formation that is at great depth.

1 22. The method of claim 1 further comprising subtracting a long-wavelength field
2 from the measured at least one component of potential fields data.

1 23. The method of claim 1 further comprising filtering the at least one component
2 of potential fields data to remove a long wavelength regional component of
3 the potential fields data prior to step (c) of claim 1.

1 24. The method of claim 14 further comprising using the difference at step (d) of
2 claim 1 for additional filtering of the long wavelength regional component.

1 25. The method of claim 1 wherein a base of the subterranean formation in the
2 determined geophysical model is expressed in terms of an ordered set of basis
3 functions.



- 1 26. The method of claim 25 wherein the set of basis functions are selected from (i)
2 half cosine functions, (ii) Legendre polynomials, (iii) polynomials; and (vi)
3 wavelets, (vii) Daubechies wavelets, and (viii) sliding boxcar functions with
4 variable widths.
- 1 27. The method of claim 25 wherein the basis functions are selected from DAUB4
2 wavelet function set.
- 1 28. The method of claim 25 wherein in step (e) of claim 1 the base of the
2 subterranean formation is not allowed to extend beyond a top of the
3 subterranean formation.
- 1 29. The method of claim 25 wherein iteratively repeating steps (c) - (e) of claim 1
2 further comprises solving for a higher basis function after solving for a lower
3 basis function.
- 1 30. The method of claim 25 wherein after each iteration low frequency
2 components are filtered out.
- 1 31. The method of claim 1 wherein iteratively repeating steps (c) - (e) further
2 comprises an integration of the determined or updated geophysical model.
- 1 32. The method of claim 31 wherein the integration of the determined or updated
2 geophysical model is carried out by a set of parallel computations.
- 1 33. The method of claim 31 wherein the integration for each parameter to be
2 inverted is chosen randomly, and further comprises:
3 (i) allowing only a small change in each parameter during each iteration;
4 and
5 (ii) applying a low-pass filter to the surface after all parameters have been
6 processed.



- 1 34. A method for determining the boundaries of an anomalous geological
2 structure, the method comprising:
3 (a) receiving a set of non-potential field data;
4 (b) determining an upper boundary of the anomalous structure using said
5 non-potential field data;
6 (c) receiving potential field data indicative of a lower boundary of said
7 anomalous structure;
8 (d) modeling a lower boundary as a weighted sum of a plurality of basis
9 functions to give a model of the lower boundary;
10 (e) obtaining a set of expected potential field data from the model of the
11 lower boundary;
12 (f) determining a plurality of weights relating the lower boundary to said
13 plurality of basis functions by iteratively adding one basis function at a
14 time based on said received potential field data; and
15 (g) determining the lower boundary of the geological structure from the
16 determined weights and the basis functions.
- 1 35. The method according to claim 34 wherein the determining the weights for
2 said plurality of basis functions further comprises:
3 (i) comparing said received potential field data to said expected potential
4 field data to obtain difference data between said received potential
5 field data and said expected potential field data; and
6 (ii) modifying the plurality of weights base upon said difference data.
- 1 36. The method according to claim 35 wherein said modifying the plurality of
2 weights includes an inversion of said potential field data.
- 1 37. The method according to claim 35 wherein ends of said upper boundary are
2 masked.
- 1 38. The method according to claim 35 wherein said potential fields data includes



2 at least one of (i) vector magnetic data, (ii) vector gravity data, (iii) tensor
3 magnetic data, and (iv) tensor gravity data.

1 39. The method of claim 34 wherein a boundary of the subterranean formation in
2 the determined geophysical model is expressed in terms of an ordered set of
3 basis functions.

1 40. The method of claim 39 wherein the set of basis functions are selected from (i)
2 half cosine functions, (ii) Legendre polynomials, (iii) polynomials; and (vi)
3 wavelets, (vii) Daubechies wavelets, and (viii) sliding boxcar functions with
4 variable widths.

1 41. A method for determining geological structures of a region of interest
2 including an anomalous formation comprising:
3 (a) obtaining and processing seismic data indicative of the region of
4 interest;
5 (b) formulating a model corresponding to the region of interest;
6 (c) using the obtained seismic data for obtaining a an upper boundary of
7 the anomalous formation in the model;
8 (d) obtaining potential fields data responsive to a lower boundary of said
9 geologic model;
10 (e) using an iterative inversion technique for determining parameters of
11 said lower boundary from said obtained potential fields data; and
12 (f) using the determined parameters of said lower boundary in processing
13 the obtained seismic data for providing a depth image of the geological
14 structures.

1 42. The method according to claim 41 wherein processing the obtained seismic
2 data further comprises at least one of (i) deriving a velocity model for a portion of the
3 region of interest, (ii) prestack migration of the obtained seismic data, and, (iii) post-
4 stack migration of the obtained seismic data.



- 1 43. The method according to claim 41 wherein using the iterative inversion
2 technique further comprises:
3 (i) predicting values of the potential fields data from the model;
4 (ii) obtaining a difference between the obtained potential fields data and
5 the predicted values of the potential fields data; and
6 (iii) modifying said parameters of said lower boundary in said geologic
7 model to reduce said difference.
- 1 44. The method according to claim 41 wherein said obtained potential fields data
2 further comprises at least one component of (i) vector magnetic data, (ii)
3 vector gravity data, (iii) tensor magnetic data, and (iv) tensor gravity data.
- 1 45. The method of claim 44 wherein the at least one component comprises at least
2 two components of potential fields data, the method further comprising
3 filtering the at least two components to give filtered data components that are
4 consistent with Laplace's equation.
- 1 46. The method of claim 44 further comprising filtering the at least one
2 component of potential fields data to remove a long wavelength regional
3 component of the potential fields data prior to step (e) of claim 41.
- 1 47. The method of claim 41 wherein a lower boundary of said geologic model is
2 expressed in terms of an ordered set of basis functions.
- 1 48. The method of claim 47 wherein the set of basis functions are selected from (i)
2 half cosine functions, (ii) Legendre polynomials, (iii) polynomials; and (vi)
3 wavelets, (vii) Daubechies wavelets, and (viii) sliding boxcar functions with
4 variable widths.
- 1 49. A method for determining a parameter of interest of an anomalous
2 subterranean formation comprising:
3 (a) measuring at least one component of potential fields data at a plurality



- 4 of locations over a region of interest including the anomalous
5 formation, said at least one component selected from (i) vector data,
6 and (ii) tensor data;
- 7 (b) acquiring seismic data over the region of interest including the
8 anomalous formation and determining therefrom an initial geophysical
9 model;
- 10 (c) for said initial geophysical model, estimating a value of said at least
11 one component of potential fields data at said plurality of locations and
12 giving estimated values of said at least one component of potential
13 fields data;
- 14 (d) determining a difference between said estimated values and said
15 measured values at said plurality of locations;
- 16 (e) updating the model of the region based on said difference;
- 17 (f) iteratively repeating steps c - e until said difference is less than a
18 predetermined value, giving an updated geophysical model;
- 19 (g) using the updated model for processing the seismic data measured to
20 obtain an improved geophysical model;
- 21 (h) using the updated geophysical model to determine the parameter of
22 interest.

1 50. The method of claim 49 wherein the anomalous formation is selected from the
2 group consisting of a salt body, a shale diapir, a magma flow and a magmatic
3 intrusion.

1 51. The method of claim 49 wherein the at least one component comprises at least
2 two components of potential fields data, the method further comprising
3 filtering the at least two components to give filtered data components that are
4 consistent with Laplace's equation.

1 52. The method of claim 49 wherein the parameter of interest is selected from (i) a
2 lower boundary of the subterranean formation, (ii) a thickness of the



subterranean formation, (iii) a density of the subterranean formation, (iv) a magnetic susceptibility of the subterranean formation, (v) a volume of the subterranean formation, (vi) overburden stress in the region of interest, (vii) effective stress in the region of interest, (viii) formation fluid pressure in the region of interest, (ix) overburden stress below the subterranean formation of interest, (x) effective stress below the subterranean formation of interest, and (xi) formation fluid pressure below the subterranean formation of interest.

53. The method of claim 49 wherein a base of the subterranean formation in the determined geophysical model is expressed in terms of an ordered set of basis functions.

54. The method of claim 53 wherein the set of basis functions are selected from (i) half cosine functions, (ii) Legendre polynomials, (iii) polynomials; and (vi) wavelets, (vii) Daubechies wavelets, and (viii) sliding boxcar functions with variable widths.

55. A method for imaging geological structures beneath an anomalous formation comprising:

- (a) obtaining seismic data over a region including the anomalous formation ;
- (b) deriving an initial geophysical model including an upper surface of said anomalous formation using said obtained seismic data;
- (c) obtaining potential fields data indicative of a lower boundary of said anomalous formation;
- (d) inverting the obtained potential fields data using the initial geophysical model for obtaining an updated geophysical model including parameters of the lower boundary of the anomalous formation, said inversion technique including sequential addition of terms in a modeling process;



- 14 (e) processing said seismic data using said updated geophysical model to
15 obtain an image of the subsurface including said lower boundary and
16 deriving therefrom an improved geophysical model; and
17 (f) inverting the obtained potential fields data using the improved
18 geophysical model to give a further refined geophysical model; and
19 (g) processing the seismic data using the refined geophysical model to
20 image geologic structures beneath the anomalous formation.

1 56. The method according to claim 55 wherein inverting the potential fields data
2 further comprises obtaining a difference between values of said potential
3 fields data and values of the potential fields data predicted from a geophysical
4 model, and modifying said geophysical model if said difference exceeds a
5 predetermined value.

1 57. The method according to claim 56 wherein the potential fields data comprises
2 at least one component of data selected from (i) vector magnetic data, (ii)
3 vector gravity data, (iii) tensor magnetic data, and, (iv) tensor gravity data.

1 58. The method of claim 57 wherein the at least one component comprises at least
2 two components of potential fields data, the method further comprising
3 filtering the at least two components to give filtered data components that are
4 consistent with Laplace's equation.

1 59. The method of claim 56 further comprising filtering the at least one
2 component of potential fields data to remove a long wavelength regional
3 component of the potential fields data prior to steps (d) and (f).

1 60. The method of claim 56 further comprising using said difference for
2 additional filtering of the long wavelength regional component.



- 1 61. The method of claim 55 wherein a base of the subterranean formation in the
2 determined geophysical model is expressed in terms of an ordered set of basis
3 functions.
- 1 62. The method of claim 61 wherein the set of basis functions are selected from (i)
2 half cosine functions, (ii) Legendre polynomials, (iii) polynomials; and (vi)
3 wavelets, (vii) Daubechies wavelets, and (viii) sliding boxcar functions with
 variable widths.
- 1 63. A method for determining formation fluid pressure in a subterranean
2 formation, the method comprising:
3 (a) obtaining a measurement of at least one component of potential fields
4 data at a plurality of locations over a region including the formation,
5 said potential fields data selected from magnetic data and gravity data;
6 (b) using seismic data acquired at a plurality of locations in said region for
7 obtaining an initial model of density in the region;
8 (c) using the initial model of density for inverting the at least one
9 component of obtained potential fields data and determining an
10 updated density model;
11 (d) using the updated density model for determining an overburden stress
12 in the formation;
13 (e) determining an effective stress in the formation from the seismic data;
14 and
15 (f) determining the formation fluid pressure from the determined
16 overburden stress and the effective stress.
- 1 64. The method of claim 63 wherein the at least one component of potential fields
2 data is at least one of: (i) a component of vector gravity field, (ii) a component
3 of tensor gravity field, (iii) a component of vector magnetic field, and, (iv) a
4 component of tensor magnetic field.



- 1 65. The method of claim 63 wherein obtaining the initial model of density further
2 comprises:
3 (i) determining seismic velocities in the region from the acquired seismic
4 data; and
5 (ii) using an empirical relation between seismic velocities and densities in
6 determining the initial model of density.
- 1 66. The method of claim 63 wherein obtaining the initial model of density further
2 comprises (i) using densities from well logs near said, and (ii) using well
3 density and velocity data to derive a locally-calibrated empirical relation for
4 converting seismic velocities to densities.
- 1 67. The method of claim 63 wherein inverting the at least one component of
2 potential fields data further comprises using the initial model of density as a
3 starting point for an iterative inversion scheme.
- 1 68. The method of claim 67 wherein inverting the at least one component of
2 potential fields data further comprises using constraints derived from the
3 initial model of density in the iterative inversion scheme.
- 1 69. The method of claim 63 wherein determining the overburden stress further
2 comprises performing a vertical integration of the updated density model.
- 1 70. The method of claim 65 wherein determining the effective stress further
2 comprises using an empirical relationship between the determined seismic
3 velocities and the effective stress.
- 1 71. The method of claim 63 wherein determining the updated model further
2 comprises:
3 (i) for said initial model, estimating a value of said at least one component
4 of potential fields data at said plurality of locations;
5 (ii) determining a difference between said estimated value and said



- 6 obtained value of said measurements at said plurality of locations;
7 (iii) updating the model of the region based on said difference; and
8 (iv) iteratively repeating steps (i) - (iii) until said difference is less than a
9 predetermined value, giving the updated geophysical model.

1 72. The method of claim 63 further comprising using the determined formation
2 fluid pressure to guide a parameter of a drilling process used for drilling a
3 borehole in the subterranean formation.

1 73. The method of claim 63 wherein inverting the at least one component of
2 potential fields data further comprises using constraints derived from the
3 initial model of density in the iterative inversion scheme.

1 74. The method of claim 63 further comprising using the determined formation
2 fluid pressure to analyze stability of a wellbore drilled in the formation.

1 75. The method of claim 70 wherein the formation has been subjected to an
2 unloading of overburden above the formation, and wherein determining the
3 effective stress further comprises a correction for a hysteresis effect related
4 thereto.

1 76. The method of claim 65 further comprising using the updated model for
2 obtaining improved seismic velocities and using said improved seismic
3 velocities in determining the effective stress.

1 77. The method of claim 63 wherein the initial model determined from the seismic
2 data includes one of (i) a topographic surface representing the land surface,
and, (ii) a bathymetric surface for marine data.

