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SENSORLESS OPTIMUM TORQUE CONTROL FOR HIGH EFFICIENCY IRONLESS PERMANENT MAGNET MACHINE

CLAIM OF BENEFIT AND INCORPORATION BY REFERENCE

[0001] This application claims priority to United States Provisional Patent Application Number 61/194,030 to *DABOUSSI*, filed September 23, 2008, entitled "SENSORLESS OPTIMUM TORQUE CONTROL FOR HIGH EFFICIENCY IRONLESS PM MACHINES", the entire disclosure of which is incorporated by reference herein.

TECHNICAL FIELD

Field of the Invention

[0002] The invention relates to a method and system for measuring the rotor position of a permanent magnet machine. More specifically, the invention relates to a method and system for using the terminal voltages and currents of an ironless permanent-magnet (PM) machine to perform sensorless motoring and generation operations.

Description of Related Art

[0003] A permanent magnet machine is a type of alternating current (AC) motor whereby power is supplied to the rotating device by means of imposing an electromagnetic field perpendicular to a field generated by permanent rotor magnets, and is illustrated by FIG. 1. To control an AC permanent magnet machine, the absolute position of the magnetic field produced by the rotor permanent magnets (PM) 102, 104 should be known at all times. The magnets' position are important for determining the stator current magnitude of the machine necessary to produce the desired torque. This operation is known as the stator current commutation. Since the magnets are rotating with respect to the stator 106, the magnets' position can be calculated by measuring the rotor absolute angular position. Absolute position sensors such as resolvers and optical encoders are typically used to measure the absolute angular position of the machine rotor. From the position information the machine angular speed can also be calculated.

[0004] Commonly used angular position sensors are mechanically coupled to the machine rotor. For some applications severe environmental conditions and/or tight

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mechanical integration concerns of such devices can lead to challenges, particularly if high operation reliability is required. To some of these applications, mechanically mounted position sensors are considered a weak link, i.e., a critical single point of failure. For cost sensitive applications, the high cost of the absolute position sensor can be a problem.

OVERVIEW

[0005] The present invention exploits both the terminal voltages and currents of an ironless permanent-magnet machine to perform sensorless electric motoring and generation operations. In estimating the electromotive force (emf) of the machine, the present invention takes advantage of the low per unit inductance of an ironless machine and uses the machine terminal voltages, which closely represent the machine emf. Some compensation is also included to offset any influence resulting from ohmic and inductive voltage drop due to the presence of stator current. Also as will be shown below, this approach takes advantage of the DC nature of the machine voltages and currents that result from the d-q rotating reference frame transformation. The present invention provides a very wide range of position and speed sensing, which allows the machine to effectively start even under very difficult starting torque conditions such as those associated with internal combustion engine. Furthermore, the present invention incorporates a torque angle optimization scheme which leads to a more efficient operation of the machine.

[0006] Embodiments of the present invention relate to a computer-implemented method for sensorless torque control by determining a rotor position using terminal voltages and currents of an ironless permanent-magnet machine to perform sensorless electric motoring and generation operations, including obtaining instantaneous terminal voltages of the machine, transforming the instantaneous terminal voltages to a zero direct axis voltage and a non-zero quadrature axis voltage, regulating the electrical frequency of the permanent-magnet machine such that the zero direct-axis voltage is adjusted to have a value of zero, determining a non-final electrical angle of the permanent-magnet machine by applying an integrator to the regulated electrical frequency of the machine, determining a final electrical angle of the machine by integrating the non-final electrical angle and an electrical angle from a previous calculation cycle, and regulating the current vector of the machine such that the current vector is perpendicular to the final electrical angle of the machine, thereby optimizing the torque of the machine.

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[0007] The embodiments of the present invention also relate to a system for sensorless torque control by determining a rotor position using terminal voltages and currents of an ironless permanent-magnet machine to perform sensorless motoring and generation operations, including means for obtaining instantaneous terminal voltages of the machine, means for transforming the instantaneous terminal voltages to a zero direct axis voltage and a non-zero quadrature axis voltage, means for regulating the electrical frequency of the permanent-magnet machine such that the zero direct-axis voltage is adjusted to have a value of zero, means for determining a non-final electrical angle of the permanent-magnet machine by applying an integrator to the regulated electrical frequency of the machine, means for determining a final electrical angle of the of the machine by integrating the non-final electrical angle and an electrical angle from a previous calculation cycle, and means for regulating the current vector of the machine such that the current vector is perpendicular to the final electrical angle of the machine, thereby optimizing the torque of the machine.

[0008] Furthermore, the embodiments of the present invention relate to a computer-readable medium for sensorless torque control by determining a rotor position using terminal voltages and currents of an ironless permanent-magnet machine to perform sensorless motoring and generation operations, including means for obtaining instantaneous terminal voltages of the machine, means for transforming the instantaneous terminal voltages to a zero direct axis voltage and a non-zero quadrature axis voltage, means for regulating the electrical frequency of the permanent-magnet machine such that the zero direct-axis voltage is adjusted to have a value of zero, means for determining a non-final electrical angle of the permanent-magnet machine by applying an integrator to the regulated electrical frequency of the machine, means for determining a final electrical angle of the of the machine by integrating the non-final electrical angle and an electrical angle from a previous calculation cycle, and means for regulating the current vector of the machine such that the current vector is perpendicular to the final electrical angle of the machine, thereby optimizing the torque of the machine.

[0009] In addition, the embodiments of the present invention relate to a computer-implemented method for sensorless torque control by determining a rotor position using terminal voltages and currents of an ironless permanent-magnet machine to perform sensorless motoring and generation operations, including obtaining instantaneous terminal voltages of the machine, transforming the instantaneous terminal voltages to a zero direct axis

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voltage and a non-zero quadrature axis voltage, using a mathematical transformation, regulating the electrical frequency of the permanent-magnet machine such that the zero direct-axis voltage is adjusted to a value of zero, determining a non-final electrical angle of the machine from the regulated electrical frequency, determining a final electrical angle of the machine by integrating the non-final electrical angle and an electrical angle from a previous calculation cycle, optimizing the electrical angle by observing the DC power supply that is in an inverter of the machine, and regulating the current vector of the machine such that the current vector is perpendicular to the final electrical angle of the machine, thereby optimizing the torque of the machine.

[0010] The embodiments of the present invention further relate to a system for sensorless torque control by determining a rotor position using terminal voltages and currents of an ironless permanent-magnet machine to perform sensorless motoring and generation operations, including means for obtaining instantaneous terminal voltages of the machine, means for transforming the instantaneous terminal voltages to a zero direct axis voltage and a non-zero quadrature axis voltage, using a mathematical transformation, means for regulating the electrical frequency of the permanent-magnet machine such that the zero direct-axis voltage is adjusted to a value of zero, means for determining a non-final electrical angle of the machine from the regulated electrical frequency, means for determining a final electrical angle of the machine by integrating the non-final electrical angle and an electrical angle from a previous calculation cycle, means for optimizing the electrical angle by observing the DC power supply that is in an inverter of the machine, and means for regulating the current vector of the machine such that the current vector is perpendicular to the final electrical angle of the machine, thereby optimizing the torque of the machine.

[0011] Moreover, the embodiments of the present invention relate to a computer-readable medium for sensorless torque control by determining a rotor position using terminal voltages and currents of an ironless permanent-magnet machine to perform sensorless motoring and generation operations, including means for obtaining instantaneous terminal voltages of the machine, means for transforming the instantaneous terminal voltages to a zero direct axis voltage and a non-zero quadrature axis voltage, using a mathematical transformation, means for regulating the electrical frequency of the permanent-magnet machine such that the zero direct-axis voltage is adjusted to a value of zero, means for determining a non-final electrical angle of the machine from the regulated electrical

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frequency, means for determining a final electrical angle of the of the machine by integrating the non-final electrical angle and an electrical angle from a previous calculation cycle, means for optimizing the electrical angle by observing the DC power supply that is in an inverter of the machine, and means for regulating the current vector of the machine such that the current vector is perpendicular to the final electrical angle of the machine, thereby optimizing the torque of the machine

BRIEF DESCRIPTION OF THE DRAWINGS

[0012] The invention is described through a preferred embodiment and the attached drawings in which:

[0013] FIG. 1 is a schematic diagram of a conventional permanent magnet machine;

[0014] FIG. 2 is a sensorless position flowchart in accordance with the preferred embodiment of the present invention;

[0015] FIG. 3 is a signal flow diagram of a phase lock loop as seen in one embodiment of the present invention;

[0016] FIG. 4 is a graphical representation of a mathematical transformation in accordance with one embodiment of the present invention; and

[0017] FIG. 5 is a flowchart of sensorless torque control of a permanent magnet machine.

DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENT

[0018] The prior art is limited to the six-step mode of current commutation where the current waveforms are square waveforms as opposed to sinusoidal waveforms. Previous sensorless methods devised to address sinusoidal excitation suffer from extreme complexity. Conventionally, a mathematical model of the system must be created, and estimation of the rotor position is accomplished using a Kalman filter. These approaches are inherently sensitive to numerical computation and require high accuracy in the model of the motor plant.

[0019] Applicants have discovered a proposed sensorless approach that overcomes the above-recited deficiencies of the prior art by eliminating the need for a mechanical device to sense the rotor's absolute angular position. Moreover, the method of the present invention

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uses a simple mathematical model to make accurate measurements of the machine's voltages and currents. Additionally, the proposed approach makes use of the machine measured variable to adjust for any variations in the machine parameters due to temperatures or other operational effects, thus improving control of the device.

[0020] The permanent magnet motor used in one embodiment of the present invention is illustrated in FIG. 1. The motor/generator of the present invention includes, among other things, ironless rotor magnets 102, 104, as well as a stator 106.

[0021] FIG. 2 illustrates a signal flow diagram for determining the electrical angle of the machine used for optimizing the torque control of the machine as seen in a preferred embodiment of the present invention. The machine model 202 includes schematic representations for three voltage sources E_a , E_b , and E_c , three resistors R_a , R_b , and R_c , and three inductors L_a , L_b , and L_c , although other configurations may be contemplated.

[0022] The motor 202 is able to receive digital signals which dictate the motor's movement. For instance, the motor is started spinning by the motor setting the current vector I_q to a very high DC magnitude. Setting the current vector I_q to a high constant value enables the magnetic field vector of the motor to align itself with the current vector I_q . At this initial time, the torque angle of the motor is near zero.

[0023] Next, as graphically represented at 204, the frequency is incrementally raised over time thereby changing the electrical angle, which then changes the angle at which the current is set. Then, the magnets in the motor track the current vector I_q as it begins to move. Having the magnets in the motor track the moving current vector I_q starts the motor spinning. Once the spinning creates a large enough emf in the machine, the position estimator over to closed loop position estimation. Also, as seen in item 202, once the machine starts turning, the instantaneous machine measured variables V_{an} , V_{bn} , and V_{cn} are obtained.

[0024] At a certain point, once the back emf coming from the motor is high enough to be a measureable quantity, an analog-to-digital converter (ADC), which is not shown, is used to convert the analog voltages coming into the motor into three digital readings of the instantaneous terminal voltages V_{an} , V_{bn} , and V_{cn} , thus beginning a calculation cycle.

[0025] Once the digital values for the instantaneous terminal voltages V_{an} , V_{bn} , and V_{cn} have been obtained, these voltages are transformed using a mathematical transformation

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206 that converts the sinusoidal machine waveform into DC quantities. This mathematical transformation can be a direct-quadrature-zero transformation (dq0), although other mathematical transformations may be contemplated. The dq0 transformation is an expression that uses the machine electrical angular position to perform the transformation.

[0026] The transformation is accomplished by establishing a d-q reference frame with the d-axis aligned with the airgap magnetic field of the machine and the q-axis in quadrature, i.e., 90° from the d-axis. If the d-axis is aligned with the magnetic field, then the frequency of rotation of the reference frame is identical to the machine magnetic field and the transformation of the machine open circuit terminal voltages will result in a zero direct axis voltage V_{de} , and a nonzero quadrature axis voltage V_{qe} , as seen in FIG. 4. The steps of the dq0 transformation will now be detailed.

[0027] A direct-quadrature-zero (dq0) transformation is a transformation of coordinates from the three-phase stationary coordinate system to the dq rotating coordinate system. This transformation is made in two steps, and is performed by :

- 1) a transformation from the three-phase stationary coordinate system to the two-phase $\alpha\beta$ stationary coordinate system; and
- 2) a transformation from the $\alpha\beta$ stationary coordinate system to the dq rotating coordinate system.

[0028] Graphical representations of these steps are shown in FIG. 4. A representation of a vector in n-dimensional space is accomplished through the product of a transpose n-dimensional vector (base) of coordinate units and a vector representation of the vector, whose elements are corresponding projections on each coordinate axis, normalized by their unit values. In three phase (i.e., three dimensional) space, it looks like this:

$$X_{abc} = [a_u \quad b_u \quad c_u] \begin{bmatrix} x_a \\ x_b \\ x_c \end{bmatrix}$$

[0029] Assuming a three-phase system ($x_0=0$), a three-phase vector representation transforms to a dq vector representation (zero-axis component is 0) through the transformation matrix T, defined as:

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$$T = \frac{2}{3} \begin{bmatrix} \cos(\omega t) & \cos(\omega t - \frac{2}{3}\pi) & \cos(\omega t + \frac{2}{3}\pi) \\ -\sin(\omega t) & -\sin(\omega t - \frac{2}{3}\pi) & -\sin(\omega t + \frac{2}{3}\pi) \end{bmatrix}$$

In other words, the transformation from $X_{abc} = \begin{bmatrix} X_a \\ X_b \\ X_c \end{bmatrix}$ (three-phase coordinates) to

$$X_{dq} = \begin{bmatrix} X_d \\ X_q \end{bmatrix}$$

(dq rotating coordinates), called Park's transformation, is obtained through the multiplication of the vector X_{abc} by the matrix T , i.e., $X_{dq} = TX_{abc}$. From the matrix T , ω is the frequency, t is time, and $\omega = d\theta/dt$. In the present invention, the variable X is actually voltage V . Conversely, the inverse transformation from dq rotating coordinates to three-phase coordinates is calculated as $X_{abc} = T'X_{dq}$, where the inverse transformation matrix is defined as:

$$T' = \begin{bmatrix} \cos(\omega t) & -\sin(\omega t) \\ \cos(\omega t - \frac{2}{3}\pi) & -\sin(\omega t - \frac{2}{3}\pi) \\ \cos(\omega t + \frac{2}{3}\pi) & -\sin(\omega t + \frac{2}{3}\pi) \end{bmatrix}$$

[0030] While the machine is turning, the processor is determining the electrical angle θ_e that is the position of the rotor with respect to the stator. The processor accomplishes this by regulating V_{de} to be equal to zero, as seen in FIG. 2. The value of V_{de} is calculated using the dq transformation as delineated above. The measurement of θ_{old} from a prior calculation cycle is initially assumed by the processor, and is also input into the Dq transformation. Next, a phase locked loop (PLL) 208 determines the electrical angle θ_e of the calculation cycle as seen in FIG. 3. The PLL includes a proportional-integral regulator 210 and an integrator 212. This type of PLL is known as type-II PLL. The PLL functions to track the angular position of the rotor electrical position by adjusting the reference frame angles such that V_{de} is kept at zero.

[0031] In a more general sense, a phase locked loop is a control system that generates a signal that has a fixed relation to the phase of a reference signal. A phase locked loop

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circuit responds to control both the frequency and the phase of the input signals of the motor, automatically raising or lowering the frequency of a controlled oscillator until it is matched to the reference in both frequency and phase. Phase locked loop mechanisms may be implemented as either analog or digital circuits. Both implementations use the same basic structure, including three basic elements: a phase detector, a variable electronic oscillator, and a feed back path which often includes a frequency divider.

[0032] A phase locked loop compares the two frequencies of two signals and produces an error signal which is proportional to the difference between the input frequencies. The error signal is then low-pass filtered and used to drive a voltage-controlled oscillator which creates an output frequency. The output frequency is fed through a frequency divider back to the input of the system, producing a negative feedback loop. If the output frequency drifts, the error signal will increase, driving the voltage-controlled oscillator (VCO) frequency in the opposite direction so as to reduce the error. Thus the output is locked to the frequency at the other input. This input is called the reference and is often derived from a crystal oscillator, which is very stable in frequency. A basic block diagram of a phase lock loop can be seen in FIG. 3.

[0033] As previously stated, the initial value of the electrical angle θ_{old} that is input into the phase locked loop is assumed from the previous calculation cycle. This value of θ_{old} and the values of the instantaneous voltages, V_{an} , V_{bn} , and V_{cn} , are run through the Dq transformation, and the values of V_{de} and V_{qe} are then output. After it is obtained, the value for V_{de} is input into block 308, and the processor then subtracts V_{de} from 0, to determine an error value. It is an error value since initially V_{de} is a non-zero value. Furthermore, a machine impedance compensator factor may also be input into block 208. This is because the terminal voltages are being used to determine V_{de} , rather than the actual back emf of the machine.

[0034] The processor assumes that the resistors R_a , R_b , and R_c of the permanent magnet (PM) machine are near zero, and thus there are only the inductors L_a , L_b , and L_c in the PM machine model. Thus, since the processor is interested in the output of the AC voltage source, but only the output of the voltage source plus the inductor is measureable, the processor determines the voltage drop across the inductor, which is $V_{Lde}=I\omega L$. The value of

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V_{Lde} is also input into the phase lock loop 212, and this value may be used to adjust the initial input value of V_{de} , thereby compensating for the inductance of the machine.

[0035] The obtained error value 216 is then processed by a proportional integral controller 310 which is called a PI filter, to obtain the electrical frequency Δf_e 218 at which the machine is rotating.

[0036] Next, the process determines a value for $\Delta\theta_e$ by multiplying Δf_e 218 by a factor of 2π , $\Delta\theta_e$ has units of radians/calculation cycle. The process then inputs the electrical angle from the previous calculation cycle, θ_{eold} and $\Delta\theta_e$ through an integrator 212, which sums these values, and outputs the value for the new electrical angle θ_{el} for the machine for that particular calculation cycle.

[0037] At this point the processor has determined the electrical angle θ_{el} of the machine, and the current regulator can now use the electrical angle θ_{el} to regulate the current vector I_q of the machine such that I_q is perpendicular to θ_{el} . The inverter imposes a current on the machine, which regulates the current vector perpendicular to the magnetic field vector, which is in phase with V_q .

[0038] In an alternate embodiment of the present invention the angle θ_{el} may be further optimized by the processor. In this particular embodiment, the processor adjusts the electrical frequency of the machine, and determines if the DC power going into the inverter of the machine is being increased or decreased. If the power decreases then the processor continues in that direction until the power increases, at which point the process has determined a value for $\Delta\theta_{eoptimize}$. The value for $\Delta\theta_{eoptimize}$ can then be input, along with the value for θ_{el} into a summation block 222 to determine an optimized electrical angle θ_e for the machine.

[0039] In another embodiment of the present invention, the output of the Dq transformation is filtered, using a low pass filter 324, to reduce the noise resulting from the machine's non-ideal waveforms and switching noise. A low-pass filter is a filter that passes low-frequency signals but attenuates (reduces the amplitude of) signals with frequencies higher than the cutoff frequency. The actual amount of attenuation for each frequency varies from filter to filter. This feed forward frequency f_{eff} may also be input into the phase lock loop 308 and be used to determine a more optimum electrical angle of the machine.

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[0040] FIG. 5 illustrates a flowchart for optimizing the torque of a permanent magnet machine in one embodiment of the present invention. In step 502, the terminal voltages of the permanent magnet machine are obtained. The terminal voltages may be obtained using an analog-to-digital converter, for example. After which, in step 504, the instantaneous terminal voltages are then transformed to a zero direct axis voltage V_{de} and a non-zero quadrature axis voltage V_{qe} using a mathematical transformation. The mathematical transformation may be the direct-quadrature-zero transformation. In step 506, the electrical frequency f_e of the machine is regulated such that the zero direct axis voltage V_{de} is adjusted to have a value of zero. Next, an electrical angle $\Delta\theta_e$ of the machine is determined by applying an integrator to the regulated electrical frequency F_e , in step 508. The final electrical angle θ_{el} is determined by applying a phase lock loop integrator to the electrical angle of the previous calculation cycle θ_{eold} and the electrical angle $\Delta\theta_e$, in step 510. Then, in step 512, the optimum torque angle $\Delta\theta_{optimize}$ is determined for the machine. In step 514, the new electrical angle of the machine θ_{enew} is obtained by applying a summation node to the final electrical angle θ_{el} and the optimized torque angle $\Delta\theta_{optimize}$. Finally, the current vector of the machine is regulated such that the current vector is perpendicular to the new electrical angle θ_{enew} of the machine, in step 516.

[0041] Thus, the above described method, system, and computer-readable medium in accordance with the embodiments of the present invention, as can now be fully appreciated, provides a very effective method for optimizing the torque control for a permanent magnet machine.

[0042] The invention has been described through a preferred embodiment. However, various modifications can be made without departing from the scope of the invention as defined by the appended claims and legal equivalents.

WHAT IS CLAIMED:

1. A method for sensorless torque control by determining a rotor position using terminal voltages and currents of an ironless permanent-magnet machine to perform sensorless motoring and/or generation operations, comprising:

obtaining instantaneous terminal voltages of the machine;

transforming the instantaneous terminal voltages to a zero direct axis voltage and a non-zero quadrature axis voltage;

regulating the electrical frequency of the permanent-magnet machine such that the zero direct-axis voltage is adjusted to have a value of zero;

determining a non-final electrical angle of the permanent-magnet machine by applying an integrator to the regulated electrical frequency of the machine;

determining a final electrical angle of the of the machine by integrating the non-final electrical angle and an electrical angle from a previous calculation cycle; and

regulating the current vector of the machine such that the current vector is perpendicular to the final electrical angle of the machine, thereby optimizing the torque of the machine.

2. A system for sensorless torque control by determining a rotor position using terminal voltages and currents of an ironless permanent-magnet machine to perform sensorless motoring and/or generation operations, comprising:

means for obtaining instantaneous terminal voltages of the machine;

means for transforming the instantaneous terminal voltages to a zero direct axis voltage and a non-zero quadrature axis voltage;

means for regulating the electrical frequency of the permanent-magnet machine such that the zero direct-axis voltage is adjusted to have a value of zero;

means for determining a non-final electrical angle of the permanent-magnet machine by applying an integrator to the regulated electrical frequency of the machine;

means for determining a final electrical angle of the of the machine by integrating the non-final electrical angle and an electrical angle from a previous calculation cycle; and

means for regulating the current vector of the machine such that the current vector is perpendicular to the final electrical angle of the machine, thereby optimizing the torque of the machine.

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3. A computer-readable medium for sensorless torque control by determining a rotor position using terminal voltages and currents of an ironless permanent-magnet machine to perform sensorless motoring and/or generation operations, comprising:

means for obtaining instantaneous terminal voltages of the machine;

means for transforming the instantaneous terminal voltages to a zero direct axis voltage and a non-zero quadrature axis voltage;

means for regulating the electrical frequency of the permanent-magnet machine such that the zero direct-axis voltage is adjusted to have a value of zero;

means for determining a non-final electrical angle of the permanent-magnet machine by applying an integrator to the regulated electrical frequency of the machine;

means for determining a final electrical angle of the of the machine by integrating the non-final electrical angle and an electrical angle from a previous calculation cycle; and

means for regulating the current vector of the machine such that the current vector is perpendicular to the final electrical angle of the machine, thereby optimizing the torque of the machine.

4. A computer-implemented method for sensorless torque control by determining a rotor position using terminal voltages and currents of an ironless permanent-magnet machine to perform sensorless motoring and/or generation operations, comprising:

obtaining instantaneous terminal voltages of the machine;

transforming the instantaneous terminal voltages to a zero direct axis voltage and a non-zero quadrature axis voltage;

regulating the electrical frequency of the permanent-magnet machine such that the zero direct-axis voltage is adjusted to a value of zero;

determining a non-final electrical angle of the machine from the regulated electrical frequency;

determining a final electrical angle of the of the machine by integrating the non-final electrical angle and an electrical angle from a previous calculation cycle;

optimizing the electrical angle by observing the DC power supply that is in an inverter of the machine; and

regulating the current vector of the machine such that the current vector is perpendicular to the final electrical angle of the machine, thereby optimizing the torque of the machine.

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5. A system for sensorless torque control by determining a rotor position using terminal voltages and currents of an ironless permanent-magnet machine to perform sensorless motoring and/or generation operations, comprising:

means for obtaining instantaneous terminal voltages of the machine;

means for transforming the instantaneous terminal voltages to a zero direct axis voltage and a non-zero quadrature axis voltage;

means for regulating the electrical frequency of the permanent-magnet machine such that the zero direct-axis voltage is adjusted to a value of zero;

means for determining a non-final electrical angle of the machine from the regulated electrical frequency;

means for determining a final electrical angle of the of the machine by integrating the non-final electrical angle and an electrical angle from a previous calculation cycle;

means for optimizing the electrical angle by observing the DC power supply that is in an inverter of the machine; and

means for regulating the current vector of the machine such that the current vector is perpendicular to the final electrical angle of the machine, thereby optimizing the torque of the machine.

6. A computer-readable medium for sensorless torque control by determining a rotor position using terminal voltages and currents of an ironless permanent-magnet machine to perform sensorless motoring and/or generation operations, comprising:

means for obtaining instantaneous terminal voltages of the machine;

means for transforming the instantaneous terminal voltages to a zero direct axis voltage and a non-zero quadrature axis voltage;

means for regulating the electrical frequency of the permanent-magnet machine such that the zero direct-axis voltage is adjusted to a value of zero;

means for determining a non-final electrical angle of the machine from the regulated electrical frequency;

means for determining a final electrical angle of the of the machine by integrating the non-final electrical angle and an electrical angle from a previous calculation cycle;

means for optimizing the electrical angle by observing the DC power supply that is in an inverter of the machine; and

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means for regulating the current vector of the machine such that the current vector is perpendicular to the final electrical angle of the machine, thereby optimizing the torque of the machine.