



MEASUREMENTS USING TUNNELLING CURRENT BETWEEN ELONGATE CONDUCTORS

Field of Invention

This invention relates to the accurate measurement and monitoring of fine
5 relative positions or displacements, eg. rotational or angular separations or
displacements, vibrations, linear separations or translations, alignments and
misalignments. Of particular, though not exclusive, interest is measurement of
angles.

Background Art

10 Known devices designed for ultra precise measurement of angles include
autocollimators, diffraction based systems and gears based systems.
Autocollimators use measurement of angular deviation to determine in turn, eg,
straightness, flatness, squareness and parallelism. Modern forms use laser diode
light sources and beamsplitters, and incorporate a micrometer in the eyepiece
15 viewing system for accurate measurement of angular displacement. Typical best
accuracies are 0.2 arcseconds, for a measuring range of 160 arcseconds.

In a known goniometer-style instrument, a pair of radial gratings rotate in
unison at a uniform speed and are scanned by a pair of reading heads. One of
these is stationary while the other moves through the angle to be measured. The
20 relative phase change between the two resultant signals is an indication of the
rotation of the moveable reading head with respect to the fixed head. Accuracy
achieved is said to be 0.1 arcsecond.

These prior devices are relatively expensive and typically rather large
instruments. Often they form a key part of another scientific apparatus, such as a
25 diffractometer, where the precise measure of angle determines the resolution and
quality of an instrument.

Accuracy of angular measurement is the subject of Zhang et al. "Improving
the Accuracy of Angle Measurement System with Optical Grating", Annals of the



CIRP Vol 43, No. 1 (1994). This paper proposes the use of index gratings with sine function transmissivity, and other enhancements, and reports an accuracy of 0.2 arcseconds with a prototype instrument.

It is an object of this invention to provide for fine measurement and
5 monitoring of relative positions or displacements, whether angular, linear or otherwise, to a satisfactory accuracy that is preferably better than that achieved with known instruments and techniques.

Summary of the Invention

The invention proposes an approach quite different from that previously
10 used, and entails monitoring the quantum tunnelling current between two proximate electrical conductors, preferably of nano dimensions. In a preferred embodiment, two arrays of aligned conductors may be used, and these may advantageously be carbon nanotubes.

The invention accordingly provides, in a first aspect, a method of measuring
15 and/or monitoring the relative position or displacement of two elements, including:

associating the elements with respective elongate electrical conductors;

disposing the conductors preferably in approximate alignment, at a mutual
separation and applying an electrical potential difference such that there is
a detectable quantum tunnelling current between them; and

20 detecting and/or measuring said quantum tunnelling current.

Preferably, the relative positions of the conductors is adjusted to determine that position at which maximum quantum tunnelling current is detected.

In a second aspect, the invention provides apparatus for use in measuring
and/or monitoring the relative position or displacement of two elements. The
25 apparatus includes a pair of elongate electrical conductors adapted to be associated with the respective elements, and means for disposing the conductors,

preferably substantially aligned in mutually parallel relationship, at a mutual separation such that a detectable quantum tunnelling current may be generated between them on the application of an electrical potential difference between the conductors.

- 5 The apparatus may further include means to apply said potential difference, and means to detect and/or measure the quantum tunnelling current between the conductors.

 Preferably, the apparatus further includes means to adjust the relative positions of the conductors to determine that position at which maximum quantum
10 tunnelling current is detected.

 The position or displacement may be one or more of a rotational or angular separation or displacement, a vibration, a linear separation or translation, an alignment and a misalignment.

 Preferably, the electrical conductors are of width 1 micron or less eg, in one
15 or more embodiments, of width in the nano-order to sub-micron range. In the latter case, the conductors may be carbon nanotubes of arbitrary helicity or radius, either single or multi-walls of carbon monofilaments, or nanowires. Alternatively, the conductors may be, eg, micron to sub-micron quasi one-dimensional conductors. In some embodiments, the conductors may be of length 1 mm or less.

20 The conductors may be associated with the aforesaid elements by being mounted in or on an insulating or semiconducting substrate, preferably flush with a surface of the substrate. The substrate may be, eg. a solid or a crystal face. The conductors may be placed along respective atomic steps on a vicinal surface.

 Advantageously, the electrical conductors are arranged in respective
25 ordered grids or arrays of electrical conductor segments, preferably wired in parallel e.g. through a single supply lead, which grids or arrays are complementary and overlaid to place the conductor segments in sufficient proximity to obtain detectable quantum tunnelling currents.

Brief Description of the Drawings

The invention will now be further described, by way of example only, with respect to the accompanying drawings, in which:

Figure 1 is a fragmentary cross-section of a first embodiment of nano-dimension device according to the invention, with the respective conductors generally aligned and electrical connections diagrammatically depicted;

Figure 2 is a modification of the embodiment of Figure 1 in which the conductors are substantially at right angles;

Figure 3 is a view similar to Figure 1 of an embodiment that utilises multiple nanotube conductors;

Figure 4 is a view similar to Figure 2 of a modification of the embodiment of Figure 3;

Figure 5 depicts a variation of the embodiment of Figure 3, formed in a particular manner; and

Figure 6 is a view similar to Figures 1 and 3 of a further embodiment of the invention that utilises an etched conductive overlay and a film applied by Langmuir-Blodgett technology.

In the embodiment of Figure 1, respective nano-dimension elongate electrically conductive wires 10, 11, of widths in the nano to sub-micron dimension range, are embedded flush in respective insulating medium substrates 12, 13. In this case, the wires are superposed in substantially aligned parallel relationship, at a separation or gap 18 in the range 2-50 Angstroms, such that when an electrical potential difference is applied by a potential source 26 across the conductors, there is a quantum tunnelling current 100 between them detectable in suitable detection circuit 27.

A suitable technique for making the embodiment is electron beam nanolithography, in which aligned conducting wire can be delineated on a semi-conducting substrate. This is described, eg. in Wilkinson et al, "Electron Beam Nanolithography", an article in the text "The Physics and Fabrication of Microstructures and Microdevices" (eds. Kelly & Weisbuch, Springer-Verlag, 1986) that describes and illustrates a set of parallel GaAs conducting wires on a semi-insulating substrate. In practical applications of the device, substrates or plates 12, 13 are associated or coupled to respective elements whose displacement or position is to be measured or monitored.

In general, tunnelling current 100 is proportional to the product of the local densities of states on a pair of adjacent electrodes (ie. conductors), or in other terms, to the sum of the square of the tunnelling matrix elements between states on both electrodes. It is also a sensitive function of the tunnelling potential and the electrode curvature. Furthermore, quantum tunnelling current is critically dependent on the spacing between the conductors because the quantum wave function decays exponentially outside the conductor surface, and the detected current will be a function of the relative angle between a pair of crossed nanotubes. The invention takes advantage of the aforementioned exponential and angular relationship in that the detected value of the tunnelling current 100 will change sharply as the longitudinal opposed surface segments of the conductor move apart with increasing rotational and/or translational misalignment or vice versa.

More particularly, suitable Schrodinger wave functions for the gap 18 are found in Kiejna & Wojciechowski, "Metal Surface Electron Physics", Pergamon (1996). It could be demonstrated from wave function analysis that the quantum tunnelling current is critically dependent on the spacing between the conductors because the quantum wave function decays exponentially outside the conductor surface, and the detected current will also be a function of the relative angle between a pair of crossed nanoconductors.

The gap 18 between the aligned opposed conductor surface segments is thought to be most appropriately in the range 2-50 Angstroms, more preferably 2-

20 Angstroms. The conductor segments may conveniently be of any length that can practicably be placed and aligned on the substrate and have leads attached, eg. in the range 1μ to 10^{-2}m long.

Gap 18 may be a partial vacuum or may be filled with an appropriate medium. Suitable arrangements for accurately maintaining the gap 18 include the use of buckyball (C_{60}) nanobearings 20, 22, or the interpositioning of a separation film of an organic medium, preferably an organic lubricant eg. cyclohexane (further disclosed below). The latter is thought to be a particularly effective approach to the maintenance of accurately parallel fine separation.

10 The adjustment means may include piezoelectric positioners of known type suitable for performing adjustments at nano dimension level.

The aforementioned effect is further enhanced if the conductors are cylindrical, as for carbon nanotubes. In the case of the grids or arrays if the conductor segments are connected in parallel, there will be an amplifying effect and this will facilitate current measurement. However, if the lines have independent connections, the grids forming the sandwich will be able to act as two dimensional arrays of point "capacitors" which can be switched on and off independently, forming a "pixelised" array of tunnelling wells.

The tunnelling current 100 will exhibit minima at one or more positions dependent on the aspect ratio (length to separation of conductor segments), and a maximum when the conductor segments of the two grids/arrays are perfectly aligned.

Figure 3 illustrates an alternative embodiment in which the electrical conductors comprise multiple parallel nanotubes 10a, 10b, 10c, 11a, 11b, 11c deposited on insulating medium substrates 12', 13'.

Procedures for producing a set of aligned nanotubes on a substrate are described, for example, at Chauvet et al, Physical Review B52, 52 (1995); de

Heer et al, Science **268**, 845 (1995); and Kiang et al, Carbon **33**, 903-914 (1995)

The properties of single wall nanotubes are described, for example, in Iijima, Nature **354**, 56-58 (1991) and Iijima et al, Nature **363**, 603-605 (1993). Carbon nanotubes of a variety of types are also described at Östling et al,
5 Physical Review B. **55**, 55 (1997).

A particular technique for producing a grid of parallel conductor segments suitable for this invention is by epitaxial deposition of nanotubes or other nano-dimension conductors on the atomic steps of a vicinal surface produced by slicing a crystal at an angle to a primary plane. The separation of the conductor
10 segments may be regular or irregular, but is most preferably parallel. Figure 5 shows a modification of the embodiment of Figure 3 in which the nanotubes are deposited in this way at the successive atomic steps 14, 15 on a stepped vicinal surface.

Figures 2 and 4 illustrate embodiments in which the respective arrays of
15 conductors of micron, submicron or nano-order dimensions when not nanotubes, are arranged with the conductors 210 of one array in or on substrate 212, extending substantially at right angles to the conductors 211 of the other array, in or on substrate 213. Instead of a right angle, the angular relationship may be at some other angle, eg. to form a diamond or rhomboidal type of two dimensional
20 lattice. In one application of such an arrangement preferably utilising a large number of conductor lines, the set of cross-over points 250 will form an artificial scattering lattice effective to scatter a beam of atoms directed parallel to the sandwich structure into the space 218 between the conductor arrays. If each line is independently electrically connected, ie they are not electrically in parallel, there
25 will be a pixellised array which is an analog of a two-dimensional "pinball game" for atoms, with predefined scattering centres.

In a variation of the scattering lattice, it may further include an array of magnetic elements forming the lattice and creating 1-dimensional domains at or between the cross-over points.

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Figure 6 is a further embodiment in which each substrate 312, 313 is atomically smooth freshly cleaved mica, and the conductors 310, 311 are formed by etching an overlay 330, 331 of gold, and then filling the interstitial grooves by application of a molecular monolayer by a Langmuir-Blodgett process. The two
5 arrays may be separated as before by a cyclohexane or other suitable organic lubricant film 318 maintained by an outer thermoshrink wrap 340.

The illustrated devices are effective electro-mechanical nanodevices. On the one hand, they may be applied to the measurement of angles, angles of rotation, rotational speed, and alignment or misalignment at microscopic and
10 macroscopic level. Rotational speed can be measured, for example, by measuring the number of current maxima per unit of time. It is thought to be capable of an accuracy of the order of 0.01 arcseconds over an operational angular range of 20° or so.

Alternatively, the illustrated devices may be used for measuring or
15 monitoring relative linear position or translation. If one substrate in the embodiments of Figures 3, 5 and 6 is translated with respect to the other, there will be a series of very sharp peaks observed in tunnelling current 100. The distance traversed will be given by the number of observed peaks times the separation between the conductors; the resolution will be of the order of the width
20 of the conductors, i.e. about 200 Angstroms with currently available nanolithography technology, but about 10-30 Angstroms with nanotubes.

The rotational and translational effects would both contribute to vibration monitoring or measurement, eg. in a seismograph.

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CLAIMS

1 **(amended)** Apparatus for measuring and/or monitoring the relative position
or displacement of two elements, including:

5 a pair of elongate electrical conductors adapted to be associated with the
respective elements; and

 means for disposing the conductors at a mutual separation with a variable
relative angle between the conductors such that a detectable quantum
tunnelling current which is a function of said relative angle may be
generated between the conductors on application of an electrical potential
10 difference between said conductors.

2 Apparatus according to claim 1, further including means to adjust the
relative positions of the conductors to determine that position at which
maximum quantum tunnelling current is detected.

3 Apparatus according to claim 2 wherein said adjustment means includes
15 one or more piezoelectric positioners.

4 **(amended)** Apparatus according to any claim 1, 2 or 3 wherein said
elongate electrical conductors are substantially aligned in mutually parallel
relationship whereby said relative angle is a measure of misalignment
between the conductors.

20 5 Apparatus according to any preceding claim, wherein said elongate
electrical conductors are arranged in respective ordered grids or arrays of
electrical conductor segments, which grids or arrays are complementary
and overlaid to place the conductor segments in sufficient proximity to
obtain detectable quantum tunnelling currents.

25 6 **(amended)** Apparatus according to claim 5 wherein the conductor
segments of each said grid or array are substantially parallel but aligned at
said relative angle to the conductor segments of the other grid(s) or

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array(s).

- 7 Apparatus according to claim 5 or 6 wherein the conductor segments of each grid or array are wired electrically in parallel.
- 8 (amended) Apparatus according to any preceding claim wherein said
5 elongate electrical conductors are of the order of micron to nanometer dimensions.
- 9 Apparatus according to claim 8 wherein said elongate electrical conductors are carbon nanotubes or nanowires, or micron to sub-micron quasi one dimensional conductors.
- 10 10 Apparatus according to any preceding claim wherein said conductors are associated with the aforesaid elements by being mounted in or on respective insulating or semiconductive substrates.
- 11 Apparatus according to claim 9 where said conductors are flush with a surface of the respective substrates.
- 15 12 Apparatus according to any preceding claim wherein each said electrical conductor is disposed along a respective atomic step on a vicinal surface providing a substrate.
- 13 Apparatus according to any one of claims 1 to 8 wherein said elongate
20 electrical conductors comprise respective segments of an integral conductive layer on an insulating or semiconductive substrate.
- 14 Apparatus according to claim 13, wherein said segments are separated and/or overlaid by a membrane or film of insulating medium.
- 15 Apparatus according to any preceding claim wherein said mutual
25 separation of opposed surface segments of said electrical conductors is in the range 2-50 Angstroms.

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- 16 Apparatus according to any preceding claim wherein said mutual separation of opposed surface segments of said electrical conductors is in the range of 2-20 Angstroms.
- 17 Apparatus according to any preceding claim, wherein said conductors are in
5 one or more conductor segments of length in the range 10^{-6} to 10^{-2} m.
- 18 Apparatus according to any preceding claim, wherein said means for disposing said conductors at said mutual separation includes an intervening film and means to confine said film.
- 19 Apparatus according to claim 18 where said intervening film is a film of an
10 organic medium, eg an organic solvent.
- 20 Apparatus according to any preceding claim, wherein said means for disposing said conductors at said mutual separation includes nanutube or buckyball (C_{60}) bearings.
- 21 Apparatus according to any preceding claim, wherein said position or
15 displacement measured and/or monitored is one or more of a rotational or angular separational displacement, a vibration, a linear separation or translation, an alignment and a misalignment.
- 22 Apparatus according to any preceding claim, said elongate electrical
20 conductors are arranged in respective ordered grids or arrays of electrical conductor segments, whereby the cross-over points of the respective arrays define a lattice of electrostatic scattering wells.
- 23 Apparatus according to claim 22, wherein said lattice further includes an array of magnetic elements forming the lattice and creating 1-dimensional domains at or between said cross-over points.
- 25 24 Apparatus according to any one of claims 1 to 23 further including means to

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apply said electrical potential difference, and means to detect and/or measure said quantum tunnelling current between said conductors.

25 **(amended)** A method of measuring and/or monitoring the relative position or displacement of two elements, including:

5 associating the elements with respective elongate electrical conductors;
disposing the conductors at a mutual separation with a variable relative angle between the conductors and applying to the conductors an electrical potential difference such that there is a detectable quantum tunnelling current between the conductors that is a function of said relative angle; and
10 detecting and/or measuring said quantum tunnelling current.

26 A method according to claim 24, further including adjusting the relative positions of the conductors to determine one or more positions at which maximum quantum tunnelling current is detected.

27 **(new)** Apparatus for measuring and/or monitoring the relative position or
15 displacement of two elements including:

respective ordered grids or arrays of elongate electrical conductor segments adapted to be associated with the respective elements; and

means for disposing the grids or arrays in a complementary and overlaid mutual separation to place the conductor segments in sufficient proximity
20 for a detectable quantum tunnelling current to be generated between the grids or arrays on application of an electrical potential difference between the grids or arrays.

28 **(new)** Apparatus according to claim 27, further including means to adjust the relative positions of the grids or arrays to determine that position at
25 which maximum quantum tunnelling current is detected.

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- 29 (new) Apparatus according to claim 27 or 28 wherein said adjustment means includes one or more piezoelectric positioners.
- 30 (new) Apparatus according to claim 27, 28 or 29 wherein the conductor segments of each said grid or array are substantially parallel but aligned at
5 an angle to the conductor segments of the other grid(s) or array(s).
- 31 (new) Apparatus according to any one of claims 27 to 30 wherein the conductor segments of each grid or array are wired electrically in parallel.
- 32 (new) Apparatus according to any one of claims 27 to 31 wherein said elongate electrical conductor segments are of the order of micron to
10 nanometer dimensions.
- 33 (new) Apparatus according to claim 32 wherein said elongate electrical conductor segments are carbon nanotubes or nanowires, or micron to sub-micron quasi one dimensional conductors.
- 34 (new) Apparatus according to any one of claims 27 to 33 wherein said
15 means for disposing said grids or arrays at said mutual separation includes an intervening film and means to confine said film.
- 35 (new) Apparatus according to claim 34 where said intervening film is a film of an organic medium, eg an organic solvent.
- 36 (new) Apparatus according to any one of claims 27 to 35 wherein said
20 means for disposing said grids or arrays at said mutual separation includes nanutube or buckyball (C₆₀) bearings.
- 37 (new) Apparatus according to any one of claims 27 to 36 wherein said position or displacement measured and/or monitored is one or more of a rotational or angular separational displacement, a vibration, a linear

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separation or translation, an alignment and a misalignment.

38 (new) Apparatus according to any one of claims 27 to 37 arranged whereby the cross-over points of the respective arrays define a lattice of electrostatic scattering wells.

5 39 (new) Apparatus according to claim 38, wherein said lattice further includes an array of magnetic elements forming the lattice and creating 1-dimensional domains at or between said cross-over points.

40 (new) Apparatus according to any one of claims 27 to 39 further including means to apply said electrical potential difference, and means to detect
10 and/or measure said quantum tunnelling current between said grids or arrays.

41 (new) Apparatus for measuring and/or monitoring the relative position or displacement of two elements, including:

15 respective ordered arrays of parallel elongate electrical conductors adapted to be associated with the respective elements; and

means for disposing the arrays at a mutual separation in which the electrical conductors of the arrays are substantially aligned in mutually parallel relationship, such that when said elements change their relative position laterally of said conductors, a detectable quantum tunnelling
20 current generated between the conductors on application of an electrical potential difference between the conductors exhibits a series of peaks that provide a measure of said relative position or displacement.

42 (new) Apparatus according to claim 41, further including means to adjust the relative positions of the conductors to determine that position at which
25 maximum quantum tunnelling current is detected.

43 (new) Apparatus according to claim 42 wherein said adjustment means

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includes one or more piezoelectric positioners.

- 44 (new) Apparatus according to claim 41, 42 or 43 wherein said elongate electrical conductors are of the order of micron to nanometer dimensions.
- 5 45 (new) Apparatus according to claim 44 wherein said elongate electrical conductors are carbon nanotubes or nanowires, or micron to sub-micron quasi one dimensional conductors.
- 46 (new) Apparatus according to any one of claims 41 to 45 wherein said conductors are associated with the aforesaid elements by being mounted in or on respective insulating or semiconductive substrates.
- 10 47 (new) Apparatus according to claim 46 where said conductors are flush with a surface of the respective substrates.
- 48 (new) Apparatus according to any one of claims 41 to 47 wherein each said electrical conductor is disposed along a respective atomic step on a vicinal surface providing a substrate.
- 15 49 (new) Apparatus according to any one of claims 41 to 48 wherein said elongate electrical conductors comprise respective segments of an integral conductive layer on an insulating or semiconductive substrate.
- 50 (new) Apparatus according to claim 49, wherein said segments are separated and/or overlaid by a membrane or film of insulating medium.
- 20 51 (new) Apparatus according to any one of claims 41 to 50 wherein said mutual separation of opposed surface segments of said electrical conductors is in the range 2-50 Angstroms.
- 52 (new) Apparatus according to any one of claims 41 to 51 wherein said mutual separation of opposed surface segments of said electrical

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conductors is in the range of 2-20 Angstroms.

53 (new) Apparatus according to any one of claims 41 to 52, wherein said conductors are in one or more conductor segments of length in the range 10^{-6} to 10^{-2} m.

5 54 (new) Apparatus according to any one of claims 41 to 53, wherein said means for disposing said conductors at said mutual separation includes an intervening film and means to confine said film.

55 (new) Apparatus according to claim 54 where said intervening film is a film of an organic medium, eg an organic solvent.

10 56 (new) Apparatus according to any one of claims 41 to 55, wherein said means for disposing said conductors at said mutual separation includes nanutube or buckyball (C_{60}) bearings.

15 57 (new) Apparatus according to any one of claims 41 to 56, wherein said position or displacement measured and/or monitored is one or more of a rotational or angular separational displacement, a vibration, a linear separation or translation, an alignment and a misalignment.

58 (new) Apparatus according to any one of claims 41 to 57 further including means to apply said electrical potential difference, and means to detect and/or measure said quantum tunnelling current between said conductors.

20 59 (new) A method of measuring and/or monitoring the relative position or displacement of two elements, including:

associating the elements with respective ordered grids or arrays of elongate electrical conductor segments;

25 disposing the grids or arrays in a complementary and overlaid mutual separation to place the conductor segments in sufficient proximity that, on

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applying to the conductors an electrical potential difference there is generated a detectable quantum tunnelling current between the grids or arrays; and

detecting and/or measuring said quantum tunnelling current.

5 60 (new) A method according to claim 59, further including adjusting the relative positions of the grids or arrays to determine one or more positions at which maximum quantum tunnelling current is detected.

61 (new) A method of measuring and/or monitoring the relative position or displacement of two elements, including:

10 associating the elements with respective ordered arrays of parallel elongate electrical conductors;

disposing the arrays at a mutual separation in which the electrical conductors of the arrays are substantially aligned in mutual parallel relationship, and applying to the conductors an electrical potential difference such that there is a detectable quantum tunnelling current generated between the conductors that exhibits a series of peaks that provide a measure of said relative position or displacement; and

15 detecting and/or measuring said quantum tunnelling current.

20 62 (new) A method according to claim 24, further including adjusting the relative positions of the arrays to determine one or more positions at which maximum quantum tunnelling current is detected.